

# Metal electron delocalization in 3d complexes estimated by positronium spin-exchange reactions

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## Abstract

The paper is the final account of a series concerning the conversion reactions promoted by ca. 70 complexes of  $\text{V}^{\text{II}}$ ,  $\text{Cr}^{\text{II}}$ ,  $\text{Cr}^{\text{III}}$ ,  $\text{Mn}^{\text{II}}$ ,  $\text{Co}^{\text{II}}$  and  $\text{Ni}^{\text{II}}$  ions. The rate constants,  $k_{\text{CR}}$ , of the reactions, measured at 278, 288, 298 and 308 K, correlate linearly with the metal electron delocalization caused by the ligands as described by the ratio  $\beta$  between the inter-electronic repulsion parameter in 3d complexes,  $B$ , and that in the free ions,  $B_0$ . The  $\beta$  values were estimated by the empirical equation  $\beta = 1 - th$ , where  $t$  and  $h$  are constants characteristic of

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the ion and ligand, respectively. The analysis of the data, limited in a previous review to the experiments carried out at 298 K, is here extended to the other three temperatures in order to ascertain if the  $t$  and  $h$  values proposed are independent of  $T$ , as it is expected. The relationship between the correlations for complexes of the same ion  $J$  in high- and low-spin configurations is also taken into consideration. An experimental equation was derived for evaluating  $k_{\text{CR}}^T$  as a function of  $T$  and  $\beta$ . The analysis of the data shows that experimental and back-calculated  $k_{\text{CR}}^T$  are in nice agreement with each other, i.e. the mean-square error of the discrepancies between the values of experimental and back-calculated rate constants are 1.3–1.4 times the mean-square error of the experimental data. This supports the statements advanced in order to explain the relationship between  $k_{\text{CR}}$  and the chemical constitution of 3d complexes. Reciprocally, the statement that the  $k_{\text{CR}}$  measurements constitute a new method for testing the metal electron delocalization in 3d complexes, gains further support. A short account on the  $o$ -Ps into  $p$ -Ps conversion reactions, their mechanisms and kinetics is also given. © 2001 Elsevier Science B.V. All rights reserved.

**Keywords:** Metal electron delocalization; 3d complexes; Positronium spin-exchange reactions

## 1. Introduction

The positron, symbol  $e^+$  (or  $\beta^+$ , if originated by radioactive decay), is the anti-electron, i.e. a particle identical to the electron,  $e^-$ , except for the sign of its charge, opposite to that of  $e^-$  [1]. The ultimate fate of  $e^+$  is to undergo annihilation by interacting with an  $e^-$ . Annihilation consists of the transformation of the masses of  $e^+$  and  $e^-$  into electromagnetic energy. The modalities of the transformation (lifetimes, angular correlations of emitted quanta, etc.) depend on the chemical environment of  $e^+$ . The annihilation modalities may consequently be used as a probe of the electronic structure of the molecules [2,3].

Positrons are generally formed with energies in the order of  $10^2$  keV by decay of certain radionuclides. After thermalization by collision with the molecules of the medium and before undergoing annihilation, a certain fraction of  $e^+$ , depending on the medium, may form bound states with the electrons. The bound states, which resemble the protium atom  $^1\text{H}$ , are called positronium atoms, Ps.

As chemical entities, Ps atoms may undergo several types of chemical reactions, which are, oxidation (leading to  $e^+$ ), addition reactions to double bonds and spin-exchange reactions, which constitute the main point of the present review.

Ps atoms may exist into two spin states: the *ortho*-state,  $o$ -Ps, and the *para*-state,  $p$ -Ps, depending on the spin orientations of the two particles: parallel in the former and anti-parallel in the latter case. Both types of Ps atoms are unstable, but with different decay modes; this makes it possible to distinguish between the two. Since  $m_s(o\text{-Ps}) = 0, \pm 1$  and  $m_s(p\text{-Ps}) = 0$ , the two types of Ps atoms are formed for statistical reasons in the ratio 3:1. Once formed,  $o$ -Ps and  $p$ -Ps atoms may be interconverted only in magnetic fields or by collisions with paramagnetic species such as many 3d complexes [3]. It will be shown (1) that the rate constants of the spin-exchange reactions promoted by 3d complexes depend on the delocalization of

the metal electrons caused by the ligands; and (2) that the rate constants of these reactions constitute a new experimental method for ascertaining the electron delocalization in complexes.

Indeed, it was found that the rate constants,  $k_{\text{CR}}$ , of the conversion reactions, CR, of *o*-Ps into *p*-Ps atoms depend on the density of unpaired metal electrons at the periphery of complexes [3]. In particular the  $k_{\text{CR}}$ s are linearly dependent on the electron delocalization caused by the ligands, as described by the ratio  $\beta = B/B_0$  between the inter-electronic repulsion parameters in the complex,  $B$ , and that in the free gaseous ions,  $B_0$ ; that is:

$$k_{\text{CR}} = a - b\beta \quad (1)$$

where  $a$  and  $b$  are the intercept and slope of the correlation line, both dependent on the coordinating ion  $J$  and temperature  $T$ . The electron delocalization increases as  $\beta \rightarrow 0$ .

It was also found that for  $T = \text{constant}$  the intercepts  $a$  of the correlation lines of the various ions are proportional to the number  $n$  of unpaired electrons [3].

The  $\beta$  ratios were evaluated by means of the following empirical equation (2), already suggested in the literature [4,5]:

$$\beta = 1 - th \quad (2)$$

where  $h$  and  $t$  are constants depending on the ligands and metal ions, respectively.

Therefore, once the parameters of the correlation line for a certain ion are known, the  $k_{\text{CR}}$  may be estimated from the corresponding  $\beta$  and, vice versa; the  $k_{\text{CR}}$  determination allows us to deduce the corresponding  $\beta$ . This reflects a new experimental method for estimating  $\beta$ .

In the present paper the  $t$  and  $h$  values of six metal ions and 20 ligands deduced from the best fit of the  $k_{\text{CR}}$ s are presented and compared with those obtained from the UV–vis measurements (Table 1) [6].

The experimental  $k_{\text{CR}}$  values at 278, 288, 298 and 308 K previously published [3] and presented in Table 2, were used. Initially the  $t$  and  $h$  values were obtained by trial and error mainly by using the data at 298 K [3]. Here the results at 278, 288 and 308 K are also taken into account. Moreover, the parameters of the correlation lines are also studied as a function of  $T$  in order to obtain a more general relationship between  $k_{\text{CR}}^T$  and  $\beta$  at the various  $T$ . The essentials of the  $\beta$  parameters and of the positronium spin-exchange reactions are summarized. Full details on the theory, experimental methods and measurements, on which the present review is based, are given in Refs. [1–3] and the papers quoted therein.

## 2. The $\beta$ parameter

The inter-electronic repulsion parameter,  $B$ , of 3d electrons in complexes is smaller than that in the free gaseous ions,  $B_0$ , due to the expansion of the 3d electron orbitals towards the donor atoms as a consequence of the overlapping of donor and 3d electron orbitals. Therefore the inter-electron repulsion between 3d electrons decreases and  $B$  also decreases.

The  $B$  values may be derived by UV–vis absorption spectroscopy; e.g. the  $\text{Cr}^{\text{III}}$  octahedral complexes are characterized in the UV–vis region by three absorption bands, whose energies ( $\text{cm}^{-1}$ ) are given by the following equations (3 and 3') [6]:

$$\bar{\nu}_1 = 10Dq \quad (3)$$

$$\bar{\nu}_{2,3} = 7.5B + 15Dq \pm (225B^2 + 100Dq^2 - 180BDq)^{1/2}/2 \quad (3')$$

where  $10Dq$  is the splitting of the fivefold degenerate  $3d$  orbitals in a triplet (lower) and a doublet (higher) caused by an octahedral ligand field and  $B$  is the inter-electronic repulsion parameter in the complex. Therefore the measurements of  $\bar{\nu}_{1-3}$  allows us to obtain  $B$ .

Jørgensen [7] suggested that the  $B/B_0 = \beta$  ratio may be estimated by the empirical Eq. (2). The  $t^*$  and  $h^*$  values resulting from the best fit of the UV–vis spectra of several complexes are given in Table 1 [4]. In the first approximation  $t^*$  and  $h^*$  values were also used to correlate  $k_{\text{CR}}$  and  $\beta$ . Indeed Eq. (2) seems to work better than it is generally believed [3], at least for its application to Ps correlations.

Another basic hypothesis, which may be controlled a posteriori, is that the  $\beta$  values of complexes formed with mixed ligand arrays, result from linear combina-

Table 1  
 $t$  and  $h$  values to be inserted in Eq. (2) in order to estimate  $\beta^a$

Ion	$t^*$	$t$	Ligand	$h^*$	$h$	Ligand	$h^*$	$h$
$\text{Co}^{\text{II}}$	0.24	0.24	6 $\text{Cl}^-$	2.0	6.3	6 acetate	—	0.98
$\text{Cr}^{\text{II}}$	—	0.13	6 $\text{CN}^-$	2.0	4.0	$\text{edta}^{4-}\text{c}$	—	1.18**
$\text{Cr}^{\text{III}}$	0.21	0.21	6 $\text{CNS}^-$	1.8	4.6	2 $\text{dien}^f$	—	1.56
$\text{Mn}^{\text{II}}$	0.07	0.07	3 $\text{en}^b$	1.5	1.56	3 $\text{gly}^-\text{g}$	—	1.28**
$\text{Ni}^{\text{II}}$	0.12	0.23	3 $\text{pn}^c$	—	1.56	2 $\text{ida}^{2-}\text{h}$	—	1.18**
$\text{V}^{\text{II}}$	0.08	0.087	6 $\text{H}_2\text{O}$	1.0	1.00	6 $\text{imH}^i$	—	0.97
			6 $\text{NH}_3$	1.4	1.4	6 $\text{dmu}^j$	—	1.30
			3 $\text{ox}^{2-}\text{d}$	1.5	1.35	2 $\text{ntp}^{6-\text{k}}$	—	0.848
			6 urea	1.2	1.33	$\text{edtp}^{8-1}$	—	1.085
						6 $\text{N}_3^-$	—	3.2

<sup>a</sup> The  $t^*$  and  $h^*$  values were deduced from best fit UV–vis spectroscopy [4]; while  $t$  and  $h$  are derived from the correlation lines between  $k_{\text{CR}}$  and  $\beta$  values.  $t^*$  and  $h^*$  are given for the sake of comparison, but in the following analysis  $t$  and  $h$  values are used. The values with \*\* were calculated by means of the average environment rule (AER). For details see the text.

<sup>b</sup> en = ethylenediamine.

<sup>c</sup> pn = propylenediamine.

<sup>d</sup>  $\text{ox}^{2-}$  = oxalate.

<sup>e</sup>  $\text{edta}^{4-}$  = ethylenediaminetetraacetate.

<sup>f</sup> dien = diethylenetriamine.

<sup>g</sup>  $\text{gly}^-$  = glycinate.

<sup>h</sup>  $\text{ida}^{2-}$  = iminodiacetate.

<sup>i</sup> imH = imidazole.

<sup>j</sup> dmu = dimethylurea.

<sup>k</sup>  $\text{ntpH}_6$  = nitrilo-tris (methylene phosphonic) acid.

<sup>l</sup>  $\text{edtpH}_8$  = ethylenediamine tetra(methylene phosphonic) acid.

tions of the  $\beta$  values of complexes formed with homogeneous arrays of ligands. The rule, referred to as the *average environment* (AER) [8], is extensively applied here. It was originally derived for estimation of mixed complexes because the complex distortion makes its experimental determination from UV–vis spectra rather troublesome. Moreover the rule was extended to include certain multidentate ligands, whose donor groups do not strongly interact among themselves, e.g. the  $\beta$  values of  $h(\text{edta}^{4-})$  and  $h(3 \text{ gly})$  ( $\text{edta}^{4-}$  = ethylenediaminetetraacetate; gly = glycinate) were considered equivalent to:

$$h(3 \text{ gly}) = \{h(6 \text{ acetate}) + h(3 \text{ en})\}/2 = 1.26 \quad (4)$$

$$h(\text{edta}^{4-}) = \{2h(6 \text{ acetate}) + h(3 \text{ en})\}/3 = 1.19 \quad (4')$$

Finally we recall that the  $h$  and  $t$  constants should be independent of the temperature  $T$ .

### 3. *o*-Ps into *p*-Ps conversion

#### 3.1. Reaction type

All the *o*-Ps into *p*-Ps conversion reactions considered here are diffusion controlled (DC). The rate constants of DC reactions are given by the Smoluchowski equation (5) [3]:

$$k = \frac{R}{1500}(r_{1,R} + r_{2,R}) \left( \frac{1}{r_{1,D}} + \frac{1}{r_{2,D}} \right) \frac{T}{\eta} \quad (5)$$

where  $r_{i,R}$  and  $r_{i,D}$  are the reaction and diffusion radii of the  $i$ th reactant;  $T$  the absolute temperature;  $R$  and  $\eta$  are the gas constant and the viscosity coefficient of the reaction medium; 1500 is a scale factor to be used in order to have  $k$  in  $\text{dm}^3 \text{mol}^{-1} \text{s}^{-1}$  if  $R$  is in  $1 \text{ erg mol}^{-1} \text{K}^{-1}$  and  $\eta$  in poise.

The following equation (6) relates the viscosity coefficients  $\eta$  to  $T$  [9]:

$$\eta = \eta_0 \exp(E_\eta/k_B T) \quad (6)$$

$\eta_0$  being a constant characteristic of the medium and  $k_B$  the Boltzmann constant. By inserting Eq. (6) into Eq. (5) one obtains Eq. (7):

$$\frac{k}{T} = \frac{R}{1500\eta_0}(r_{1,R} + r_{2,R}) \left( \frac{1}{r_{1,D}} + \frac{1}{r_{2,D}} \right) \exp\left(-\frac{E_\eta}{k_B T}\right) \quad (7)$$

Therefore the rate constants of DC reactions, measured in a given medium at various  $T$ , must fulfill the following two conditions:

1.  $k_{\text{CR}}$  must be linearly dependent on  $T/\eta$  and the straight line must have zero intercept (Eq. (5))
2. the activation energy derived from the slope of  $\ln(k/T)$  versus  $1/T$  must match the activation energy of the viscosity coefficient of the reaction medium.

Table 2  
Experimental,  $k_{\text{exp}}$ , and back-calculated,  $\bar{k}_{\text{calc}}$ , rate constants of CR in  $\text{dm}^3 \text{mol}^{-1} \text{ns}^{-1}$ , at various  $T^a$

Complexes	$h_L$	$\beta$	$k_{\text{CR}}$	278 K	288 K	298 K	308 K
$[\text{V}^{\text{II}}(\text{H}_2\text{O})_6]^{2+}$	1.00	0.913	Exp.	$0.38 \pm 0.01$	$0.55 \pm 0.02$	$0.63 \pm 0.02$	$0.91 \pm 0.02$
			Calc.	0.41	0.55	0.72	0.91
$[\text{V}^{\text{II}}\text{edta}]^{2-}$	1.18	0.897	Exp.	$0.35 \pm 0.02$	$0.40 \pm 0.04$	$0.72 \pm 0.05$	$0.77 \pm 0.07$
			Calc.	0.48	0.64	0.85	1.09
$[\text{V}^{\text{II}}\text{dien}_2]^{2+}$	1.56	0.864	Exp.	—	—	$1.15 \pm 0.09$	—
			Calc.	—	—	1.11	—
$[\text{V}^{\text{II}}(\text{NCS})_6]^{4-}$	4.6	0.600	Exp.	$2.0 \pm 0.2$	$2.6 \pm 0.1$	$3.5 \pm 0.1$	$4.5 \pm 0.1$
			Calc.	1.78	2.43	3.25	4.28
$[\text{V}^{\text{II}}(\text{CN})_6]^{4-}$	4.0	0.652	Exp.	—	—	$2.5 \pm 0.2$	—
			Calc.	—	—	2.83	—
$[\text{V}^{\text{II}}(\text{imH})_6]^{2+}$	0.97	0.916	Exp.	$0.45 \pm 0.02$	$0.62 \pm 0.05$	$0.76 \pm 0.03$	$0.97 \pm 0.06$
			Calc.	0.40	0.53	0.69	0.88
$\bar{k}_{\text{exp}}$	$\bar{\rho} = 1.6$			0.10	0.06	0.10	0.07
$\bar{k}_{\text{calc}}$				0.13	0.15	0.20	0.20
$[\text{Cr}^{\text{III}}(\text{H}_2\text{O})_6]^{2+}$	1.00	0.870	Exp.	$1.21 \pm 0.24$	$1.92 \pm 0.18$	$2.76 \pm 0.09$	$3.39 \pm 0.28$
			Calc.	1.47	1.99	2.66	3.46
$[\text{Cr}^{\text{III}}\text{edtaH}_2\text{O}]^{2-}$	1.18	0.847	Exp.	—	—	$3.20 \pm 0.22$	—
			Calc.	—	—	2.88	—
$[\text{Cr}^{\text{III}}\text{urea}_6]^{2+}$	1.33	0.827	Exp.	$1.78 \pm 0.05$	$2.35 \pm 0.03$	$3.17 \pm 0.05$	$3.84 \pm 0.27$
			Calc.	1.69	2.29	3.07	3.99
$[\text{Cr}^{\text{III}}(\text{NCS})_4(\text{H}_2\text{O})]^{2-}$	3.40	0.558	Exp.	$2.95 \pm 0.18$	$4.32 \pm 0.06$	$5.42 \pm 0.06$	$7.2 \pm 0.1$
			Calc.	3.05	4.16	5.59	7.34
$*[\text{Cr}^{\text{III}}(\text{CN})_6]^{4-}$	4.00	0.480	Exp.	—	—	$3.25 \pm 0.10$	—
			Calc.	—	—	3.16	—
$[\text{Cr}^{\text{III}}(\text{imH})_6]^{2+}$	0.97	0.874	Exp.	$1.50 \pm 0.04$	$2.08 \pm 0.10$	$2.67 \pm 0.06$	$3.20 \pm 0.14$
			Calc.	1.45	1.96	2.62	3.41
$\bar{k}_{\text{exp}}$	$\bar{\rho} = 0.93$			0.15	0.11	0.13	0.21
$\bar{k}_{\text{calc}}$				0.15	0.11	0.20	0.15

<sup>a</sup>Is configuration  $S > 1/2$ ; see Section 4.3

Table 2 (Continued)

Complexes	$h_L$	$\beta$	$k_{CR}$	278 K	288 K	298 K	308 K
$[Cr^{III}(H_2O)_6]^{3+}$	1.00	0.790	Exp. Calc.	0.55 ± 0.05 0.63	0.73 ± 0.03 0.84	1.01 ± 0.09 1.10	1.36 ± 0.06 1.41
$[Cr^{III}urea_6]^{3+}$	1.33	0.721	Exp. Calc.	1.00 ± 0.10 0.96	1.43 ± 0.07 1.29	1.74 ± 0.06 1.71	2.16 ± 0.04 2.23
$[Cr^{III}(NH_3)_6]^{3+}$	1.40	0.706	Exp. Calc.	1.06 ± 0.01 1.03	1.44 ± 0.07 1.39	1.79 ± 0.02 1.84	2.06 ± 0.07 2.40
$[Cr^{III}ox_3]^{3-}$	1.35	0.716	Exp. Calc.	0.98 ± 0.03 0.99	1.39 ± 0.05 1.33	1.63 ± 0.09 1.75	2.06 ± 0.07 2.29
$[Cr^{III}en_3]^{3+}$	1.56	0.672	Exp. Calc.	1.22 ± 0.09 1.20	1.66 ± 0.05 1.62	2.09 ± 0.06 2.14	2.80 ± 0.08 2.80
$[Cr^{III}(CN)_6]^{3-}$	4.00	0.160	Exp. Calc.	3.86 ± 0.07 3.65	5.40 ± 0.07 4.99	6.85 ± 0.12 6.70	8.43 ± 0.18 8.83
$[Cr^{III}(NCS)_6]^{3-}$	4.6	0.034	Exp. Calc.	4.20 ± 0.37 4.25	6.15 ± 0.18 5.82	8.15 ± 0.17 7.82	10.7 ± 0.02 10.32
$[Cr^{III}en_2(H_2O)_2]^{3+}$	1.37	0.712	Exp. Calc.	0.85 ± 0.02 1.01	1.34 ± 0.07 1.35	1.80 ± 0.03 1.79	2.23 ± 0.07 2.33
$[Cr^{III}en_2ox]^+$	1.49	0.687	Exp. Calc.	1.09 ± 0.02 1.13	1.75 ± 0.02 1.52	2.21 ± 0.06 2.01	2.78 ± 0.06 2.63
$[Cr^{III}edtaH_2O]^-$	1.19	0.752	Exp. Calc.	0.82 ± 0.05 0.82	1.17 ± 0.01 1.09	1.42 ± 0.02 1.43	1.87 ± 0.03 1.86
$[Cr^{III}ox_2(H_2O)_2]^-$	1.23	0.742	Exp. Calc.	0.79 ± 0.04 0.86	1.25 ± 0.05 1.16	1.53 ± 0.04 1.52	1.69 ± 0.04 1.98
$[Cr^{III}dien(H_2O)_3]^{3+}$	1.27	0.733	Exp. Calc.	0.90 ± 0.03 0.91	1.26 ± 0.05 1.21	1.72 ± 0.13 1.60	2.13 ± 0.03 2.09
$[Cr^{III}en_2(NCS)_2]^+$	2.55	0.464	Exp. Calc.	2.19 ± 0.01 2.19	3.56 ± 0.24 2.99	4.96 ± 0.13 4.00	5.94 ± 0.10 5.25
$[Cr^{III}(NH_3)_2(NCS)_4]^-$	3.53	0.258	Exp. Calc.	2.85 ± 0.24 3.18	3.75 ± 0.12 4.34	5.07 ± 0.18 5.83	6.66 ± 0.11 7.68
$[Cr^{III}edta(CN)_2]^{3-}$	2.18	0.542	Exp. Calc.	— —	— —	3.26 ± 0.03 3.30	— —
$[Cr^{III}edta(CN)H_2O]^{2-}$	1.68	0.647	Exp. Calc.	— —	— —	2.31 ± 0.05 2.37	— —
$[Cr^{III}(H_2O)_5Cl]^{2+}$	1.87	0.607	Exp. Calc.	1.24 ± 0.05 1.51	1.93 ± 0.11 2.04	2.63 ± 0.15 2.72	3.39 ± 0.17 3.57

Table 2 (Continued)

Complexes	$h_L$	$\beta$	$k_{CR}$	278 K	288 K	298 K	308 K
$[Cr^{III}en_2Cl_2]^+$	3.09	0.351	Exp. Calc.	–	–	4.9 ± 0.2 5.00	–
$[Cr^{III}en_2(H_2O)Cl]^2+$	2.22	0.534	Exp. Calc.	–	–	3.44 ± 0.12 3.37	–
$[Cr^{III}edtp]^3-$	1.085	0.772	Exp. Calc.	0.65 ± 0.04 0.72	0.86 ± 0.04 0.96	1.22 ± 0.02 1.26	1.50 ± 0.02 1.63
$[Cr^{III}(ntp)_2]^9-$	0.848	0.822	Exp. Calc.	0.52 ± 0.01 0.48	0.70 ± 0.05 0.63	0.89 ± 0.02 0.81	1.18 ± 0.09 1.04
$[Cr^{III}(imH)_6]^3+$	0.97	0.796	Exp. Calc.	0.53 ± 0.05 0.61	0.80 ± 0.02 0.80	1.10 ± 0.01 1.04	1.39 ± 0.05 1.34
$[Cr^{III}(H_2O)_4Cl_2]^+$	2.75	0.422	Exp. Calc.	–	–	4.5 ± 0.2 4.37	–
$[Cr^{III}(NH_3)_5N_3]^2+$	1.70	0.643	Exp. Calc.	1.30 ± 0.10 1.34	1.73 ± 0.09 1.81	2.27 ± 0.09 2.40	2.87 ± 0.16 3.14
$[Cr^{III}en_2(N_3)_2]^+$	2.09	0.561	Exp. Calc.	1.84 ± 0.02 1.73	2.48 ± 0.12 2.35	3.29 ± 0.07 3.13	4.08 ± 0.07 4.11
$\frac{k_{exp}}{J_{calc}}$	$\bar{\rho} = 2.3$			0.11 0.12	0.09 0.23	0.11 0.27	0.10 0.34
$[Mn^{II}(H_2O)_6]^2+$	1.00	0.930	Exp. Calc.	0.58 ± 0.03 0.60	0.84 ± 0.02 0.82	1.06 ± 0.03 1.10	1.38 ± 0.02 1.41
$[Mn^{II}ida_2]^2-$	1.18	0.917	Exp. Calc.	0.63 ± 0.03 0.69	0.88 ± 0.02 0.95	1.26 ± 0.03 1.27	1.45 ± 0.03 1.64
$[Mn^{II}gly_3]^-$	1.28	0.911	Exp. Calc.	0.98 ± 0.03 0.74	1.28 ± 0.03 1.01	1.59 ± 0.03 1.35	1.87 ± 0.08 1.74
$[Mn^{II}urea_6]^2+$	1.33	0.907	Exp. Calc.	0.78 ± 0.02 0.77	1.11 ± 0.01 1.05	1.39 ± 0.01 1.41	1.70 ± 0.06 1.81
$[Mn^{II}en_3]^2+$	1.56	0.891	Exp. Calc.	0.85 ± 0.05 0.88	1.20 ± 0.06 1.21	1.67 ± 0.05 1.62	2.25 ± 0.10 2.10
$[Mn^{II}(imH)_6]^2+$	0.97	0.932	Exp. Calc.	0.58 ± 0.02 0.58	0.89 ± 0.01 0.80	1.16 ± 0.04 1.07	1.56 ± 0.04 1.37
$[Mn^{II}dmu_6]^2+$	1.30	0.909	Exp. Calc.	0.61 ± 0.06 0.75	0.99 ± 0.06 1.03	1.25 ± 0.06 1.37	1.68 ± 0.06 1.78
$*[Mn^{II}(CN)_6]^{4-}$	4.0	0.72	Exp. Calc.	–	–	2.35 ± 0.18 2.35	3.12 ± 0.35 3.07



Table 2 (Continued)

Complexes	$h_L$	$\beta$	$k_{CR}$	278 K	288 K	298 K	308 K
$\bar{\epsilon}_{exp}$ $\Delta_{calc}$ *Is configuration; $S = 1/2$ , see Section 4.3	$\bar{\rho} = 2.1$			0.14 0.11	0.04 0.11	0.07 0.10	0.14 0.14
$[Co^{II}(H_2O)_6]^{2+}$	1.00	0.760	Exp. Calc.	1.30 ± 0.06 1.14	1.74 ± 0.03 1.48	2.21 ± 0.07 1.89	2.71 ± 0.10 2.37
$[Co^{II}ntp_2]^{10-}$	0.848	0.797	Exp. Calc.	0.97 ± 0.03 0.98	1.35 ± 0.06 1.26	1.79 ± 0.06 1.58	2.36 ± 0.08 1.96
$[Co^{II}edtp]^{6-}$	1.085	0.746	Exp. Calc.	1.01 ± 0.08 1.20	1.43 ± 0.06 1.57	1.87 ± 0.05 2.00	2.30 ± 0.01 2.52
$[Co^{II}edtaH_2O]^{2-}$	1.18	0.717	Exp. Calc.	1.38 ± 0.04 1.33	1.85 ± 0.02 1.74	2.41 ± 0.05 2.24	3.02 ± 0.10 2.84
$[Co^{II}urea]^{2+}$	1.33	0.681	Exp. Calc.	1.58 ± 0.02 1.48	2.00 ± 0.03 1.96	2.54 ± 0.08 2.53	3.13 ± 0.09 3.24
$[Co^{II}gly_3]^{-}$	1.28	0.693	Exp. Calc.	1.51 ± 0.04 1.43	2.06 ± 0.05 1.89	2.47 ± 0.02 2.44	2.86 ± 0.03 3.10
$[Co^{II}dien_2]^{2+}$	1.56	0.626	Exp. Calc.	1.58 ± 0.06 1.72	2.20 ± 0.03 2.29	2.66 ± 0.03 2.99	3.27 ± 0.07 3.84
* $[Co^{II}(CN)_5H_2O]^{3-}$	3.50	0.160	Exp. Calc.	3.49 ± 0.18 3.72	4.82 ± 0.09 5.10	6.74 ± 0.10 6.81	8.95 ± 0.35 8.98
$[Co^{II}imH_6]^{2+}$	0.97	0.767	Exp. Calc.	0.96 ± 0.08 1.11	1.27 ± 0.03 1.44	1.63 ± 0.03 1.83	2.18 ± 0.10 2.29
$[Co^{II}dmu_6]^{2+}$	1.30	0.688	Exp. Calc.	1.50 ± 0.04 1.45	2.17 ± 0.08 1.92	2.61 ± 0.09 2.48	3.13 ± 0.07 3.16
$\bar{\epsilon}_{exp}$ $\Delta_{calc}$ *Is configuration $S = 1/2$ ; see Section 4.3	$\bar{\rho} = 1.3$			0.08 0.14	0.16 0.23	0.14 0.18	0.29 0.25
$[Ni^{II}ntp_2]^{10-}$	0.848	0.805	Exp. Calc.	1.47 ± 0.13 1.54	1.85 ± 0.10 2.03	2.38 ± 0.07 2.61	2.99 ± 0.16 3.27
$[Ni^{II}edtaH_2O]^{2-}$	1.18	0.729	Exp. Calc.	1.87 ± 0.08 1.67	2.61 ± 0.12 2.21	3.15 ± 0.15 2.88	3.96 ± 0.05 3.64
$[Ni^{II}(H_2O)_6]^{2+}$	1.00	0.770	Exp. Calc.	1.44 ± 0.02 1.60	1.99 ± 0.05 2.11	2.58 ± 0.03 2.73	3.27 ± 0.10 3.44

Table 2 (Continued)

Complexes	$h_L$	$\beta$	$k_{CR}$	278 K	288 K	298 K	308 K
$[Ni^{II}urea]^{2+}$	1.33	0.694	Exp. Calc.	$1.82 \pm 0.01$ <i>1.73</i>	$2.37 \pm 0.06$ <i>2.30</i>	$2.96 \pm 0.06$ <i>3.00</i>	$3.70 \pm 0.07$ <i>3.81</i>
$[Ni^{II}(NCS)_2H_2OedtaH_2]^{2-}$	2.42	0.443	Exp. Calc.	$2.23 \pm 0.08$ <i>2.17</i>	$3.02 \pm 0.06$ <i>2.93</i>	$3.84 \pm 0.17$ <i>3.87</i>	$4.65 \pm 0.06$ <i>5.01</i>
$[Ni^{II}(NCS)_2H_2Ogly]^-$	2.32	0.466	Exp. Calc.	$1.92 \pm 0.01$ <i>2.13</i>	$2.95 \pm 0.04$ <i>2.87</i>	$3.81 \pm 0.08$ <i>3.79</i>	$4.59 \pm 0.03$ <i>4.90</i>
$[Ni^{II}dien_2]^{2+}$	1.57	0.639	Exp. Calc.	$1.80 \pm 0.03$ <i>1.83</i>	$2.45 \pm 0.07$ <i>2.44</i>	$3.12 \pm 0.07$ <i>3.19</i>	$4.03 \pm 0.12$ <i>4.07</i>
$[Ni^{II}(dmu)_6]^{2+}$	1.30	0.700	Exp. Calc.	$1.59 \pm 0.16$ <i>1.72</i>	$2.26 \pm 0.12$ <i>2.29</i>	$3.00 \pm 0.15$ <i>2.98</i>	$3.83 \pm 0.27$ <i>3.78</i>
$[Ni^{II}(imH)_6]^{2+}$	0.97	0.777	Exp. Calc.	$1.45 \pm 0.04$ <i>1.59</i>	$1.82 \pm 0.02$ <i>2.10</i>	$2.71 \pm 0.04$ <i>2.71</i>	$3.55 \pm 0.11$ <i>3.41</i>
$[Ni^{II}edtp]^{6-}$	1.085	0.750	Exp. Calc.	$1.56 \pm 0.05$ <i>1.63</i>	$2.22 \pm 0.06$ <i>2.16</i>	$2.89 \pm 0.12$ <i>2.80</i>	$3.57 \pm 0.17$ <i>3.54</i>
$[Ni^{II}gly_3]^-$	1.28	0.706	Exp. Calc.	$2.01 \pm 0.06$ <i>1.71</i>	$2.57 \pm 0.02$ <i>2.27</i>	$3.16 \pm 0.08$ <i>2.96</i>	$3.86 \pm 0.09$ <i>3.75</i>
$\bar{\bar{\epsilon}}_{exp}$				0.08	0.16	0.10	0.13
$\bar{\bar{\Delta}}_{calc}$	$\bar{\rho} = 1.5$			0.18	0.19	0.14	0.21

<sup>a</sup> The  $\beta$  values were calculated with  $\tau$  and  $h$  constants of Table 1; the  $h_i$  and then  $\beta$  values of mixed complexes were estimated by means of the average environment rule (AER). The  $\bar{K}_{calc}$  were evaluated by using Eq. (13), eventually corrected for the spin configuration of the complexes.  $\bar{\epsilon}_{exp}$  and  $\bar{\Delta}_{calc}$  are, respectively, the mean-square experimental error and the mean-square difference between experimental and back-calculated rate constants for each set of complexes at various  $T$ .  $\rho^T$  is the mean of the ratio between  $\bar{\Delta}_{calc}$  and  $\bar{\epsilon}_{exp}^T$  at each  $T$  and  $\bar{\rho}$  is the mean of  $\rho^T$ . For details see the text.



out of three collisions, will the *o*-Ps into *p*-Ps conversion reaction occur without violating the spin conservation law and only in 1/4 of these collisions will *p*-Ps formation result (see above).

In conclusion, the conversion reaction probability is 1/4 according to spin flip and 1/12 according to the catalyzed exchange.

All the paramagnetic complexes considered here have  $S > 1/2$ , excluding the  $[\text{Mn}^{\text{II}}(\text{CN})_6]^{4-}$  and  $[\text{Co}^{\text{II}}(\text{CN})_5\text{H}_2\text{O}]^{3-}$  low spin, ls, complexes, for which  $S = 1/2$ . Therefore, the spin flip mechanism is effective only in these two cases. They are discussed separately in the following together with that of the  $[\text{Cr}^{\text{II}}(\text{CN})_6]^{4-}$  complex ( $S = 1$ ), also of ls type. All the other complexes considered are of the high spin, hs, type [13].

### 3.3. Rate constants $k_{\text{CR}}$ of Ps conversion reactions promoted by 3d complexes

The occurrence of SE reactions does not depend only on the statistical factor discussed above, but also on the spin–spin coupling during the M and Ps contact time in the collisional complex. In the early stages of Ps chemistry and occasionally since then this factor was tentatively correlated with the number  $n$  of unpaired electrons [17], but without success however. Recently it was suggested that  $k_{\text{CR}}$  should not directly depend on  $n$ , but rather on the electron spin density at the periphery of the complexes, where the collisions between the complex species and Ps atoms occur [18]. In turn, the spin density, i.e. the electron density, should depend on both:

1. the ligand capability to delocalize the unpaired metal electrons;
2. and the tendency of metal ions to spread out their electrons towards the donor atoms and finally towards the periphery of the complexes.

In conclusion, it was argued that the  $k_{\text{CR}}$  of complexes of the ion  $J$  with the same electron configuration should be linearly correlated with  $\beta$  (Eq. (9)):

$$k_{\text{CR},Jl}^T = a_J^T - b_J^T \beta_{Jl} \quad (9)$$

where  $k_{\text{CR},Jl}^T$  is the rate constant of CR promoted by the complex of the ion  $J$  with the ligand  $l$  at the temperature  $T$ ;  $\beta_{Jl}$  is the electron delocalization in the complex;  $a_J^T$  and  $b_J^T$  are the intercept and slope of the correlation line, respectively, at the temperature  $T$ .

As a consequence,  $k_{\text{CR}}^T$  is expected to be proportional to  $n$  only for  $\beta = 0$ , i.e. only the intercepts  $a_J^T$  of the correlation lines should be directly proportional to the number  $n$  of unpaired metal electrons.

At first, the  $k_{\text{CR}}$  values were correlated with the  $\beta$  values calculated with Eq. (2) and the  $t^*$  and  $h^*$  values of Table 1 derived by the best fit of the UV–vis absorption data [4]. However, it was immediately recognized that better correlations could be obtained if the  $h^*$  values of  $\text{Cl}^-$ ,  $\text{CN}^-$  and  $\text{NCS}^-$  ligands (2.0; 2.0 and 1.8, respectively) were substituted by 6.3; 4.0 and 4.6 (Table 1) [3,18,19]. The  $h^*(6 \text{ urea})$  and  $h^*(3 \text{ ox}^{2-})$  constants were also slightly modified to 1.33 and 1.35, respectively, instead of 1.20 and 1.50. The new  $h$  values are shown in Table 1. In order to explain the discrepancies between  $h^*$  and  $h$ , it was tentatively suggested

Table 3

Intercepts,  $a_J^T$ , slopes,  $b_J^T$  ( $\text{dm}^3 \text{mol}^{-1} \text{ns}^{-1}$ ), and correlation coefficients,  $r$ , of the correlation lines, at various  $T$ , between  $k_{\text{CR}}^T$  (in  $\text{dm}^3 \text{mol}^{-1} \text{ns}^{-1}$ ) and  $\beta$  for hs complexes of the ion  $J^a$

Ion	Parameter	278 K	288 K	298 K	308 K
$\text{Cr}^{\text{III}}$ $n = 3$	$a_J$	$4.38 \pm 0.09$	$6.25 \pm 0.16$	$8.22 \pm 0.17$	$10.54 \pm 0.24$
	$b_J$	$4.82 \pm 0.13$	$6.86 \pm 0.25$	$9.03 \pm 0.28$	$11.65 \pm 0.36$
	$r$	$-0.9938$	$-0.9881$	$-0.9894$	$-0.9914$
$\text{V}^{\text{II}}$ $n = 3$	$a_J$	$5.10 \pm 0.31$	$6.59 \pm 0.57$	$8.17 \pm 0.56$	$11.47 \pm 0.70$
	$b_J$	$5.18 \pm 0.37$	$6.68 \pm 0.67$	$8.21 \pm 0.69$	$11.65 \pm 0.83$
	$r$	$-0.9949$	$-0.9900$	$-0.9862$	$-0.9950$
$\text{Co}^{\text{II}}$ $n = 3$	$a_J$	$4.03 \pm 0.16$	$5.70 \pm 0.21$	$7.90 \pm 0.25$	$10.56 \pm 0.38$
	$b_J$	$3.78 \pm 0.23$	$5.45 \pm 0.30$	$7.85 \pm 0.37$	$10.89 \pm 0.55$
	$r$	$-0.9850$	$-0.9882$	$-0.9913$	$-0.9896$
$\text{Mn}^{\text{II}}$ $n = 5$	$a_J$	$7.32 \pm 3.43$	$9.42 \pm 3.26$	$13.67 \pm 3.35$	$18.02 \pm 4.30$
	$b_J$	$7.22 \pm 3.76$	$9.19 \pm 3.56$	$13.49 \pm 3.67$	$17.86 \pm 4.71$
	$r$	$-0.6521$	$-0.7556$	$-0.8547$	$-0.8615$
$\text{Ni}^{\text{II}}$ $n = 2$	$a_J$	$2.90 \pm 0.30$	$4.38 \pm 0.35$	$5.48 \pm 0.27$	$6.44 \pm 0.34$
	$b_J$	$1.70 \pm 0.44$	$2.96 \pm 0.51$	$3.56 \pm 0.40$	$3.86 \pm 0.50$
	$r$	$-0.7893$	$-0.8871$	$-0.9479$	$-0.9322$
$\text{Cr}^{\text{II}}$ $n = 4$	$a_J$	$5.73 \pm 0.59$	$8.43 \pm 0.29$	$11.00 \pm 0.43$	$14.15 \pm 0.21$
	$b_J$	$4.94 \pm 0.74$	$7.37 \pm 0.36$	$9.43 \pm 0.56$	$12.45 \pm 0.27$
	$r$	$-0.9781$	$-0.9976$	$-0.9929$	$-0.9995$
$\chi^T$	Exp. <sup>b</sup>	$1.47 \pm 0.04$	$2.02 \pm 0.06$	$2.72 \pm 0.02$	$3.57 \pm 0.06$
	Calc. <sup>c</sup>	$1.47 \pm 0.01$	$2.02 \pm 0.01$	$2.71 \pm 0.01$	$3.58 \pm 0.03$

<sup>a</sup>  $n_J$  is the number of its unpaired electrons.  $\chi^T$ , in  $\text{dm}^3 \text{mol}^{-1} \text{ns}^{-1}$  (number of electron)<sup>-1</sup>, is the slope of the correlation line of  $a_J^T$  vs.  $n_J$  at any given  $T$ . The extrapolations were carried out without any constraint both for  $a_J^T$  and  $b_J^T$ . Details in the text.

<sup>b</sup>  $\chi_{\text{exp}}^T$  are the experimental slopes of  $a_J^T$  vs.  $n_J$ .

<sup>c</sup>  $\chi_{\text{calc}}^T$  are the slopes of  $a_J^T$  vs.  $n_J$  back-calculated by means of Eq. (11').

that the UV–vis measurements probe the metal electron delocalization to donor atoms, while the  $k_{\text{CR}}$  test that at the periphery of the complexes (see below). The point will be reconsidered later on.

The intercepts  $a_J^T$  and slopes  $b_J^T$  of the correlation lines between  $k_{\text{CR}}^T$  and  $\beta$  for complexes of the various ions are given in Table 3 as a function of  $T$ .

As anticipated at  $T = \text{constant}$  the intercepts  $a_J^T$  of the correlation lines are proportional to the number  $n_J$  of unpaired electrons of the ion  $J$  (see Table 3 and Fig. 1), i.e.:

$$a_J^T = n_J \chi^T \quad (10)$$

By extrapolating the experimental  $a_J^T$  of Table 3 versus  $n_J$  using the least mean-squares method with the obvious constraint that the straight line must pass through the Cartesian axes origin, the  $\chi^T$  values shown in Table 3 (items  $\chi_{\text{exp}}^T$ ) were obtained.

#### 4. The final refinement of the correlations

Analysis of the experimental data summarized above was restrained mainly to results obtained at 298 K [3]; the  $h$  and  $t$  values used for calculating  $\beta$  (Table 1) were also chiefly derived from experiments carried out at this temperature [3]. The present objectives are:

1. to see if the  $t$  and  $h$  values derived from the  $k_{\text{CR}}$  at 298 K (Table 2) may also satisfactorily be used at other temperatures, as expected;
2. to find the dependence  $a_f^T$  and  $b_f^T$  on  $T$ ;
3. to test the relationship between the correlation parameters for low spin, ls, and high spin, hs, complexes of the same ion and meantime to check the ratio between the reaction statistical factors for complexes with  $S = 1/2$  and  $S > 1/2$  (3:1) (Section 3.2);
4. to compare the experimental  $k_{\text{CR}}^T$  with those  $\bar{k}_{\text{CR}}^T$  calculated by using the  $a_f^T$  and  $b_f^T$  values obtained by extrapolating the experimental  $a_f^T$  and  $b_f^T$  versus  $T$  (see below Eqs. (11) and (12))
5. to analyze the discrepancies  $\Delta$  between the experimental,  $k_{\text{CR}}$ , and evaluated,  $\bar{k}_{\text{CR}}$ , rate constants in order to compare them with the experimental errors,  $\varepsilon_{\text{exp}}$ , of the  $k_{\text{CR}}$  measurements.

##### 4.1. Reliability of $t$ and $h$ values

The  $\beta$  values of the various complexes are given in Table 2, while the  $t$  and  $h$  values used are shown in Table 1. The reliability of the hypothesis that  $t$ ,  $h$  and then  $\beta$  are independent of  $T$ , may be checked by means of the correlation coefficients  $r$  of the straight lines extrapolating  $k_{\text{CR}}$  versus  $\beta$  at various  $T$ . There is no evidence (Table 3) that the  $r$  values depend on  $T$ , with the exclusion, perhaps, of  $\text{Mn}^{\text{II}}$

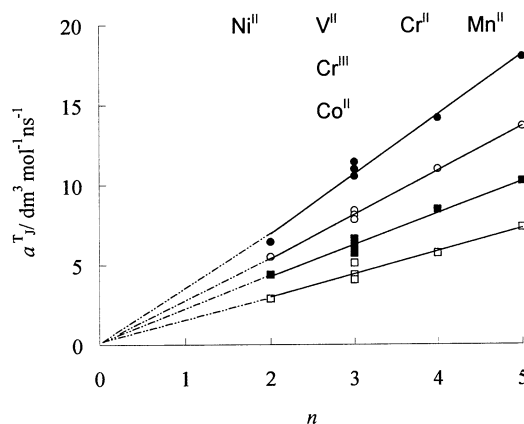


Fig. 1. Intercepts  $a_f^T$  of the various correlation lines versus the number  $n$  of unpaired electrons ( $5 \geq n > 1$ ) of the named ions in the hs configuration: □ 278; ■ 288; ○ 298; ● 308 K. Data from Table 3.

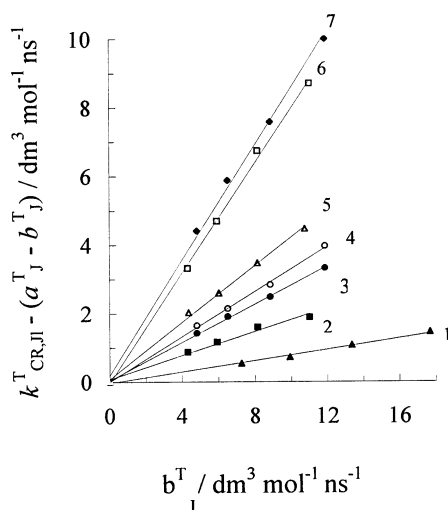


Fig. 2. Plots of Eq. (9') for various complexes. The plots support the statement that the products  $t_J$  by  $h_l$ , suggested here, and therefore  $\beta$ , do not depend on  $T$ : 1  $[\text{Mn}^{\text{II}}(\text{ida})_2]^{2-}$ ; 2  $[\text{Co}^{\text{II}}(\text{imH})_6]^{2+}$ ; 3  $[\text{Cr}^{\text{III}}\text{urea}_6]^{3+}$ ; 4  $[\text{Cr}^{\text{III}}\text{en}_3]^{3+}$ ; 5  $[\text{V}^{\text{II}}(\text{NCS})_6]^{4-}$ ; 6  $[\text{Co}^{\text{II}}(\text{CN})_5\text{H}_2\text{O}]^{3-}$ ; 7  $[\text{Cr}^{\text{III}}(\text{CN})_6]^{3-}$ .  $k_{\text{CR}}^T$  from Table 2;  $a_J^T$  and  $b_J^T$  from Table 4.

complexes ( $r$  values are worse at 278 and 288 K) possibly because of the small  $k_{\text{CR}}$  values at 278 and 288 K.

The statement may also be checked by writing Eq. (9) as shown below (Eq. (9')):

$$k_{\text{CR},Jl}^T - (a_J^T - b_J^T) = b_J^T t_J h_l \quad (9')$$

A plot of the left-hand side of Eq. (9') versus  $b_J^T$  for any given complex  $Jl$  at various  $T$ , should be a straight line passing through the Cartesian origin, provided that the product  $t_J$  by  $h_l$  is independent of  $T$ . As an example some plots of this type are shown in Fig. 2; the plots support the statement, at least, within the  $T$  interval checked and the experimental error. Later on it will be shown that the parameter  $t$  is also independent of the spin configuration of the complexes.

#### 4.2. Intercepts and slopes of the correlation lines between $k_{\text{CR}}$ and $\beta$ as a function of $T$

The Smoluchowski equation (7), which applies to  $k_{\text{CR}}^T$  values, may also be extended to  $b_J^T$  and  $a_J^T$  and therefore to  $\chi^T$ . For  $\chi^T$ , one obtains Eq. (11):

$$\frac{\chi^T}{T} = \alpha_0 \exp(-E_a/k_B T) \quad (11)$$

where  $E_a$  is the activation energy of  $\chi^T$  and  $\alpha_0$  is a constant given in  $\text{dm}^3 \text{mol}^{-1} \text{ns}^{-1}$  (number of electron) $^{-1}$ . The activation energy  $E_a$  of  $\chi^T$ , obtained from the

slope of the straight line extrapolating  $\ln(\chi^T/T)$  versus  $1/T$ , is  $2243 \pm 11 \text{ mol K}^{-1}$ , corresponding to  $E_a = 0.194 \pm 0.001 \text{ eV}$ .  $E_a$  is practically equal to the activation energy  $E_\eta$  of the viscosity coefficient of the reaction medium, water in the present case ( $E_\eta = 0.184 \pm 0.004$ ) [3]. The intercept,  $\ln \alpha_0$ , of the straight line is  $2.826 \pm 0.039$  (1.4%), i.e.  $\alpha_0 = 16.86 \pm 0.66 \text{ dm}^3 \text{ mol}^{-1} \text{ ns}^{-1} (\text{number of electron})^{-1}$ .

The  $\chi^T$  values back-calculated with the following equation:

$$\chi^T = 16.87T \exp(-2243/T) \quad (11')$$

are equal (see  $\chi_{\text{calc}}^T$  in Table 3) to the measured ones within the experimental error, i.e. within  $\pm 0.01 \text{ dm}^3 \text{ mol}^{-1} \text{ ns}^{-1} (\text{number of electron})^{-1}$ .

In order to obtain  $b_J^T$ , since  $a_J^T$  at  $T = \text{constant}$  is given by  $n_J \chi^T$ , the experimental  $k_{\text{CR},J}^T$  were extrapolated versus  $\beta$  with the constraint that the straight lines must pass through the points  $P(0, n_J \chi^T)$ , i.e. the intercept  $a_J^T$  of the correlation line was constrained to the value  $n_J \chi^T$ . The  $\chi^T$  values were calculated by means of Eq. (11') and the parameters  $\alpha_0$  and  $E_a$  quoted above (see also Table 3). The estimated  $b_J^T$  values are shown in Table 4 (items  $b_{J,\text{exp}}^T$ ).

The  $b_{J,\text{exp}}^T$  of each ion  $J$  may be extrapolated versus  $T$  by means of Eq. (12), also derived from Eq. (7):

Table 4

Slopes  $b_J^T$  (same units as in Table 3) of the straight lines extrapolating  $k_{\text{CR},J}^T$  vs.  $\beta$  for hs complexes of the ion  $J$  with the ligand  $l$  as a function of  $T^a$

Ion	Parameters of the extrapolating line		278 K	288 K	298 K	308 K
$\text{Cr}^{\text{III}}$ $n_J = 3$	$a_J^T = n_J \chi^T$ $b_J^T$		4.41	6.04 <sub>s</sub>	8.12	10.72
		Exp. <sup>b</sup>	$4.83 \pm 0.04$	$6.52 \pm 0.08$	$8.86 \pm 0.09$	$11.88 \pm 0.12$
		Calc. <sup>c</sup>	$4.78 \pm 0.01$	$6.59 \pm 0.03$	$8.80 \pm 0.005$	$11.78 \pm 0.010$
$\text{V}^{\text{II}}$ $n_J = 3$	$a_J^T = n_J \chi^T$ $b_J^T$		4.41	6.04 <sub>s</sub>	8.12	10.72
		Exp. <sup>b</sup>	$4.37 \pm 0.09$	$6.03 \pm 0.11$	$8.15 \pm 0.10$	$10.75 \pm 0.14$
		Calc. <sup>c</sup>	$4.37 \pm 0.03$	$6.02 \pm 0.03$	$8.13 \pm 0.05$	$10.77 \pm 0.08$
$\text{Co}^{\text{II}}$ $n_J = 3$	$a_J^T = n_J \chi^T$ $b_J^T$		4.41	6.04 <sub>s</sub>	8.12	10.72
		Exp. <sup>b</sup>	$4.32 \pm 0.07$	$5.93 \pm 0.08$	$8.16 \pm 0.09$	$11.02 \pm 0.13$
		Calc. <sup>c</sup>	$4.30 \pm 0.01$	$6.00 \pm 0.01$	$8.20 \pm 0.01$	$10.99 \pm 0.02$
$\text{Mn}^{\text{II}}$ $n_J = 5$	$a_J^T = n_J \chi^T$ $b_J^T$		7.35	10.08	13.55	17.85
		Exp. <sup>b</sup>	$7.26 \pm 0.05$	$9.92 \pm 0.05$	$13.36 \pm 0.05$	$17.67 \pm 0.06$
		Calc. <sup>c</sup>	$7.26 \pm 0.01$	$9.96 \pm 0.01$	$13.39 \pm 0.01$	$17.68 \pm 0.01$
$\text{Ni}^{\text{II}}$ $n_J = 2$	$a_J^T = n_J \chi^T$ $b_J^T$		2.94	4.03	5.42	7.14
		Exp. <sup>b</sup>	$1.76 \pm 0.07$	$2.45 \pm .09$	$3.48 \pm 0.06$	$4.85 \pm 0.10$
		Calc. <sup>c</sup>	$1.74 \pm 0.01$	$2.49 \pm 0.01$	$3.49 \pm 0.01$	$4.80 \pm 0.02$
$\text{Cr}^{\text{II}}$ $n_J = 4$	$a_J^T = n_J \chi^T$ $b_J^T$		5.88	8.06	10.84	14.28
		Exp. <sup>b</sup>	$5.13 \pm 0.10$	$6.91 \pm 0.07$	$9.24 \pm 0.11$	$12.62 \pm 0.04$
		Calc. <sup>c</sup>	$5.07 \pm 0.01$	$6.98 \pm 0.02$	$9.40 \pm 0.02$	$12.44 \pm 0.05$

<sup>a</sup> The constraints that the intercepts must be  $n_J \chi_0^T$  are imposed.  $n_J$  and  $\chi_0^T$  in Table 3 (details in the text).

<sup>b</sup> The experimental  $b_J^T$  values obtained under the conditions given above.

<sup>c</sup> The backcalculated  $b_J^T$  values were obtained by means of Eq. (12) with the  $\gamma_{0J}$  and  $E_{b,J}$  given in Table 5.



Table 5

The parameters  $\gamma_{0,J}$  and  $E_{b,J}$  of Eq. (12), obtained by linear extrapolation of  $\ln(b_J^T/T)$  vs.  $1/T$ , are given together with the correlation coefficients,  $r$ , of the straight lines<sup>a</sup>

	$r$	$\ln \gamma_{0,J}$	$\gamma_{0,J}$	$E_{b,J}/k_B$ (K)	$E_{b,J}$ (eV)
Cr <sup>III</sup>	0.9996	4.1422	62.94	$2281 \pm 45$	$0.197 \pm 0.000$
V <sup>II</sup>	1.0000	4.0448	57.10	$2279 \pm 9$	$0.197 \pm 0.001$
Co <sup>II</sup>	0.9998	4.4096	82.24	$2385 \pm 27$	$0.206 \pm 0.002$
Mn <sup>II</sup>	1.0000	4.4376	84.57	$2247 \pm 8$	$0.194 \pm 0.001$
Ni <sup>II</sup>	0.9994	4.3126	74.63	$2610 \pm 66$	$0.225 \pm 0.006$
Cr <sup>II</sup>	0.9990	4.1478	63.29	$2266 \pm 73$	$0.196 \pm 0.006$
		$\ln \alpha_0$	$\alpha_0$	$E_a/k_B$ (K)	$E_a$ (eV)
$\chi$	1.0000	2.8257	16.87	$2243 \pm 11$	$0.194 \pm 0.001$

<sup>a</sup> The  $r_{2;0.01}$  and  $r_{2;0.001}$  for two degrees of freedom at 0.01 and 0.001 levels of risk are 0.9900. The analogous parameters  $\alpha_0$  and  $E_a$  of Eq. (11) are given in the last line.

$$b_J^T = \gamma_0 T \exp(-E_{b,J}/k_B T) \quad (12)$$

Table 5 shows the parameters  $\gamma_0$  and  $E_{b,J}$  of Eq. (12) obtained by extrapolating  $\ln(b_{J,\text{exp}}^T/T)$  (Table 4) versus  $1/T$  by means of the least-squares method. With the exception, perhaps, of the Ni<sup>II</sup> ion, the  $E_{b,J}$  activation energies are compatible with the activation energy of the viscosity coefficient of the reaction medium, water in the present case ( $0.184 \pm 0.005$  eV). The discrepancy presented by Ni<sup>II</sup> may be due both to the small variations of the  $k_{\text{CR}}$  of Ni<sup>II</sup> complexes with  $\beta$  and to their experimental error.

Table 4 shows the slopes  $b_{J,\text{calc}}^T$ , calculated using Eq. (12) and the pertinent  $\gamma_{0,J}$  and  $E_{b,J}$  values of Table 5. They agree rather well with experimental values.

#### 4.3. Correlations between $k_{\text{CR}}$ and $\beta$ for high- and low-spin complexes

We assume that  $t$  is dependent on the ion valence, but independent of the spin configuration of the complexes, and that, in order to adapt the correlation lines of hs to ls complexes, the intercepts  $a$  and slopes  $b$  of the hs correlation lines must be:

1. multiplied by  $\bar{n}_J/n_J$ , where  $\bar{n}_J$  and  $n_J$  are the number of unpaired electrons of the ion  $J$  in ls and hs configurations, respectively;
2. and, if  $S = 1/2$  in ls configuration,  $a$  and  $b$  must also be multiplied by 3 in order to take into account the different reaction probabilities for  $S = 1/2$  and  $S > 1/2$  (1/4: 1/12, respectively) (see Section 3.2).

The  $[\text{Cr}^{\text{II}}(\text{CN})_6]^{4-}$ ,  $[\text{Mn}^{\text{II}}(\text{CN})_6]^{4-}$ , and  $[\text{Co}^{\text{II}}(\text{CN})_5\text{H}_2\text{O}]^{3-}$  complexes (see Table 6) may illustrate the different cases offered by the normalization of the  $k_{\text{CR}}$  values of the ls complexes to the  $k_{\text{CR}}$  values predicted by the correlation lines for hs complexes with the same  $\beta$ . Calling  $F$  the normalization factor, one has:

1.  $[\text{Cr}^{\text{II}}(\text{CN})_6]^{4-}$ : Since  $n_J = 4$  and  $\bar{n}_J = 2$ ,  $F$  is 2. This is the simplest case.
2.  $[\text{Mn}^{\text{II}}(\text{CN})_6]^{4-}$ : Since  $n_J = 5$  and  $\bar{n}_J = 1$ ,  $F$  is 5/3; the factor 5 accounts for the different number of unpaired electrons in hs and ls configurations (5:1), while

1/3 takes into account the different reaction probabilities for  $S > 1/2$  and  $S = 1/2$  (Section 3.2).

3.  $[\text{Co}^{\text{II}}(\text{CN})_5\text{H}_2\text{O}]^{3-}$ : Since  $n_J = 3$ ,  $\bar{n}_J = 1$  and the ratio of the reaction probabilities in hs and ls configurations for  $S = 1/2$  is 1/3, the normalization factor  $F$  is 1. The case is analogous to the previous one, but here the two parts of the normalization factor fortuitously compensate each other.

Reciprocally, the parameters  $a$  and  $b$  of the correlation lines for ls complexes may be obtained by multiplying those of the hs configurations (Table 4) by  $\bar{n}_J/n_J$  and also by 3 if  $\bar{n}_J = 1$ . Table 2 shows that the experimental  $k_{\text{CR}}$  values of the ls complexes are in agreement with their estimates, suggested here.

#### 4.4. Comparison between experimental and back-calculated rate constants

The back-calculated  $\bar{k}_{\text{CR},J}^T$  values for complexes of the ions mentioned in the hs configurations may be obtained by means of the following equation (13) derived by combining Eqs. (1), (2), (10) and (11) and Eq. (12):

$$\bar{k}_{\text{CR},J}^T = n_J \alpha_0 T \exp(-E_a/k_B T) - \gamma_{0,J} T [\exp(-E_{b,J}/k_B T)](1 - th) \quad (13)$$

$n_J$  being the number of unpaired electrons of the ion  $J$  in the hs configuration. For low spin complexes see Section 4.3.

By using the  $\alpha_0$ ,  $E_a$ ,  $\gamma_{0,J}$ ,  $E_{b,J}$  values of Table 5 and the  $t$  and  $h$  values of Table 1, the  $\bar{k}_{\text{CR},J}^T$  values shown in Table 2 (in italic) were derived.

The mean-square difference  $\bar{\Delta}_J^T$  between calculated and experimental rate constants are reported in Table 2 for the complexes of each ion  $J$  at various  $T$ . The mean-square,  $\bar{\varepsilon}_{\text{exp}}^T$ , of the experimental errors, and the mean values,  $\bar{\rho}_J$ , of  $\rho = \Delta_J^T/\varepsilon_{\text{exp}}^T$  are also inserted in Table 2.

It may be seen that  $\bar{\rho}_J$  is no larger than 1.9. Thus, by assuming that:

$$\bar{\Delta} = (\bar{\varepsilon}_{\text{exp}}^2 + \bar{\varepsilon}_{\text{calc}}^2)^{1/2} \quad (14)$$

where  $\bar{\varepsilon}_{\text{calc}}$  is the mean-square error of the rate constants  $\bar{k}_{\text{CR},J}^T$  estimated by Eq. (13), one obtains:

Table 6

High- and low-spin configurations of  $\text{Cr}^{\text{II}}$  ( $d^4$ ),  $\text{Mn}^{\text{II}}$  ( $d^5$ ) and  $\text{Co}^{\text{II}}$  ( $d^7$ ) ions together with the corresponding  $S$  values.  $\beta$  values are also shown together with the factors  $F$  which normalize the  $k_{\text{CR}}$  of ls configurations (Table 2) to those of the complexes in hs configurations<sup>a</sup>

Complex	ls	hs	$\beta$	$F$
$[\text{Cr}^{\text{II}}(\text{CN})_6]^{4-}$	$t_{2g}^4; S = 1$	$t_{2g}^3 e_g^1; S = 2$	0.480	2
$[\text{Mn}^{\text{II}}(\text{CN})_6]^{4-}$	$t_{2g}^5; S = 1/2$	$t_{2g}^3 e_g^2; S = 5/2$	0.720	5/3
$[\text{Co}^{\text{II}}(\text{CN})_5\text{H}_2\text{O}]^{3-}$	$t_{2g}^6 e_g^1; S = 1/2$	$t_{2g}^5 e_g^2; S = 3/2$	0.160	1

<sup>a</sup> Slopes and intercepts of the hs correlation lines are given in Table 4. The normalized  $k_{\text{CR}}$  are in nice agreement with those of the hypothetical complexes of the same ions  $J$  with the same  $\beta$  (Table 2).

Table 7

Slopes and correlation coefficients of the straight lines extrapolating  $\bar{k}_{\text{CR},Jl}^T$  vs.  $k_{\text{CR},Jl}^T$  at 278, 288, 298 and 308 K (see Fig. 3(a–d))<sup>a</sup>

$T$ (K)	Slopes	$r$	$\nu$
278	$1.012 \pm 0.011$	0.987	56
288	$0.973 \pm 0.011$	1.000	56
298	$0.986 \pm 0.008$	0.991	66
308	$1.013 \pm 0.009$	0.992	56

<sup>a</sup> The correlation coefficients  $r$  for 66 and 56 degrees of freedom ( $\nu$ ) at 0.001 level of risk are:  $r_{66;0.001} < r_{56;0.001} = 0.41$ .

$$\frac{\bar{A}}{\bar{\varepsilon}_{\text{exp}}} = \left( 1 + \frac{\bar{\varepsilon}_{\text{calc}}^2}{\bar{\varepsilon}_{\text{exp}}^2} \right)^{1/2} = \bar{\rho} \quad (15)$$

where  $\bar{\varepsilon}_{\text{calc}}$  is the mean square error of the calculated  $\bar{k}_{\text{CR},Jl}^T$ . Since  $\rho \leq 1.9$  (see Table 2), it follows that  $\bar{\varepsilon}_{\text{calc}}$  is not larger than 1.6 times  $\bar{\varepsilon}_{\text{exp}}$ .

Finally, slopes and correlation coefficients of the straight lines extrapolating  $\bar{k}_{\text{CR},Jl}^T$  versus  $k_{\text{CR},Jl}^T$  at various  $T$  with the constraint that the straight lines must pass through the origin (see Table 7 and Fig. 3(a–d)) are practically equal to 1.

## 5. Conclusions

The main achievements from the data reviewed here [3] may be summarized as follows: the rate constants,  $k_{\text{CR},Jl}^T$  of the conversion reactions promoted at the temperature  $T$  by the complexes of the 3d ion  $J$  with the ligands  $l$ , may be estimated by Eq. (9). The  $a_J^T$  and  $b_J^T$  values may be calculated by means of Eqs. (11') and (12) within 278 and 308 K, but the  $T$  interval may probably be enlarged on both sides by at least 5 K.

The electron delocalization  $\beta_{Jl}$ , given by the  $B/B_0$  ratio between the inter-electronic repulsion parameters in complex,  $B$ , and that in the free ions,  $B_0$ , may be estimated by means of the an empirical equation (Eq. (2)), already suggested in the literature.

The constants  $t$  and  $h$ , presented in Table 1, were obtained by assuming the following conditions:  $h(6 \text{ H}_2\text{O}) = 1$  and  $\beta = 0$  as  $h$  attains the value  $1/t$  [3]. While the first condition is also common to that used in the best fit of UV–vis absorption spectra [7], the second is new for  $t$  and  $h$  values derived from  $k_{\text{CR}}$  measurements [3]. The constants  $t$  and  $h$  of Table 1 give the best results as far as the correlation between  $k_{\text{CR}}$  and  $\beta$  values are concerned.

The differences between  $h$  and  $h^*$  values (Table 1) may be ascribed to the fact that the UV–vis spectra probe the electron delocalization towards the donor atoms, while  $k_{\text{CR}}$  should test that at the periphery of the complexes. However, one cannot disregard the consequences of the different mathematical constraint applied to the product  $t$  by  $h$  in the two cases [3].

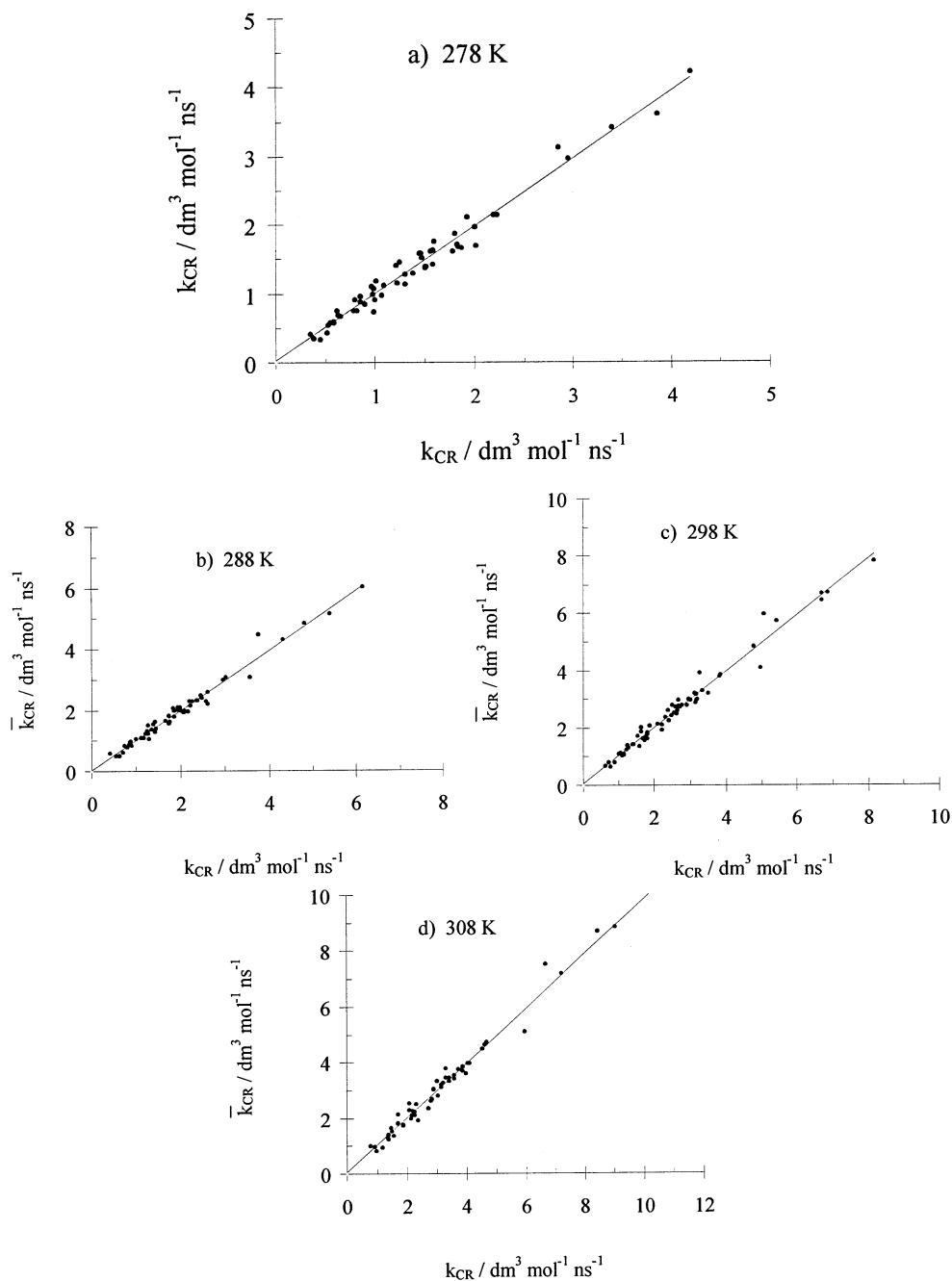


Fig. 3. Plots of  $\bar{k}_{CR}$  vs.  $k_{CR}$  at various  $T$ : (a) 278; (b) 288; (c) 298; (d) 308 K. The slopes of the extrapolating straight lines are given in Table 7 together with their correlation coefficients  $r$  and the degrees of freedom  $\nu$ .

The  $t$ ,  $h$ ,  $a_J^T$  and  $b_J^T$  values proposed in Tables 1 and 4 constitute a congruent system of data, from which  $k_{\text{CR}}^T$  may be evaluated, once the  $\beta$  values are known. Vice versa, the  $\beta$  values of the complexes may be estimated by means of the corresponding  $k_{\text{CR}}^T$  values and Eq. (9').

Eq. (13) valid for complexes of the ion  $J$  in the hs configuration may be adapted to complexes in the ls configuration by multiplying both terms on the right side of Eq. (9') by  $\bar{n}_J/n_J$ , where  $\bar{n}_J$  and  $n_J$  are the number unpaired electrons of the ion in ls and hs configurations respectively, and, eventually, by 3, if  $\bar{n}_J = 1$ .

In conclusion, four main points may be stated:

1. Eq. (2) seems to work better than previously believed;
2. the explanation advanced to justify the dependence of the *o*-Ps into *p*-Ps conversion rate constants on the chemical constitution of the paramagnetic 3d complexes causing the spin exchange, should be regarded as a new successful outcome of ligand field theory;
3. the  $t$  value of Eq. (2) does not depend on the spin configuration;
4. a new experimental method is suggested for determining the electron delocalization in 3d complexes caused by ligands.

From a more general point of view, one may say that the chemistry of exotic atoms is not esoteric, i.e. an isolated branch of the chemistry, but, on the contrary, it involves the core of many fundamental chemical problems. Moreover the positronium chemistry of 3d complexes, including the redox reactions which were not considered here [3], is by no means the lone point of impact between positronium and chemistry; other examples are surface chemistry, radiation chemistry, polymer chemistry, solid state chemistry, micelle chemistry and even biological chemistry, since micelles are the simplest model of cellular structures [2]. The apparent novelty and strangeness of this research is a product both of the present fragmentation of the sciences and also of the difficulty to dominate nearby fields of chemistry.

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## References

- [1] K.S. Krane, *Introductory Nuclear Physics*, Wiley, New York, 1987.
- [2] D.N. Schrader, Y.C. Jean, *Positronium Chemistry*, Elsevier, New York, 1988.
- [3] E. Lazzarini, *Progr. React. Kinet. Mechanism* 24 (1999) 1, and references cited therein.
- [4] B.N. Figgis, *Introduction to Ligand Field*, Interscience, London, 1966, p. 245.

- [5] J.E. Huheey, E.A. Keiter, R.L. Keiter, *Inorganic Chemistry*, Harper Collins, New York, 1993, p. 413.
- [6] Y.-s. Dou, *J. Chem. Educ.* 67 (1990) 134.
- [7] C.K. Jørgensen, *Modern Aspects of the Ligand Field Theory*, North Holland, Amsterdam, 1971, p. 346.
- [8] B.N. Figgis, *Introduction to Ligand Field*, Interscience, London, 1966, p. 246.
- [9] E.A. Moelwyn-Hughes, *Physical Chemistry*, Pergamon, Oxford, 1964, p. 715.
- [10] A.L. Fantola-Lazzarini, E. Lazzarini, *J. Phys. B.* 22 (1989) 541.
- [11] A.L. Fantola-Lazzarini, E. Lazzarini, *Gazz. Chim. Ital.* 122 (1992) 99.
- [12] E.J. Hart, M. Anbar, *The Hydrated Electron*, Wiley, New York, 1970.
- [13] F.A. Cotton, G. Wilkinson, *Advanced Inorganic Chemistry*, first ed., Interscience, New York, 1962, p. 569.
- [14] R.A. Ferrel, *Phys. Rev* 110 (1958) 1355.
- [15] J. Green, J. Lee, *Positronium Chemistry*, Academic, New York, 1964, p. 52.
- [16] G. Porter, M.R. Wright, *Discuss. Faraday Soc.* 27 (1959) 18.
- [17] J. Green, J. Lee, *Positronium Chemistry*, Academic, New York, 1964, p. 82.
- [18] A.L. Fantola-Lazzarini, E. Lazzarini, *Struct. Chem.* 3 (1992) 407.
- [19] A.L. Fantola-Lazzarini, E. Lazzarini, M. Mariani, *J. Chem. Soc. Faraday Trans.* 92 (1996) 1395.