

UTD Analysis of a Shaped Subreflector in a Dual Offset-Reflector Antenna System

Kyutae Lim, Hwang Ryu, Sangseol Lee, and Jaehoon Choi

Abstract— The geometrical theory of diffraction (GTD) is known as an efficient high-frequency method for the analysis of electrically large objects such as a reflector antenna. However, it is difficult to obtain geometrical parameters in order to apply GTD to an arbitrary-shaped reflector, especially a subreflector. In this paper, the geometrical parameters of an arbitrary shaped subreflector for the uniform theory of diffraction (UTD) analysis are derived based on differential geometry. The radiation patterns of various subreflector types, including hyperboloidal and a shaped subreflector, are evaluated by UTD. The computed result for the hyperboloidal reflector agrees well with that obtained by uniform asymptotic theory (UAT).

Index Terms— Geometrical theory of diffraction, reflector antennas.

I. INTRODUCTION

IN analyzing a dual offset-reflector antenna, the accurate calculation of a subreflector pattern is essential since it strongly affects the far-field pattern of the antenna system. The geometrical theory of diffraction (GTD) has many advantages in analyzing a subreflector over the well-known physical optics (PO) approach [1]. GTD not only gives more accurate results over a wide angle, but also requires less computation time than PO. On the other hand, there is difficulty in finding geometrical parameters, including the second-order derivatives on the reflector surface.

Keller's original GTD has the serious problem of producing inaccurate results at the shadow boundaries [2]. To overcome this difficulty, two uniform versions of GTD, the uniform theory of diffraction (UTD) [3], [4] and the uniform asymptotic theory (UAT) [5], [6], have been developed. UAT has been developed based on the Ansatz of Lewis *et al.* [7]. In UTD, Keller's diffraction coefficients have been modified by using the Pauli-Clemmow's method of steepest descent [8], [9].

The main difficulty that lies in the GTD analysis of an arbitrary shaped subreflector is the evaluation of geometrical parameters based on differential geometry. Lee *et al.* [10] presented the UAT solution for an arbitrary subreflector. Despite the wide usage of UTD, the UTD solution for an arbitrary subreflector has not yet been formulated.

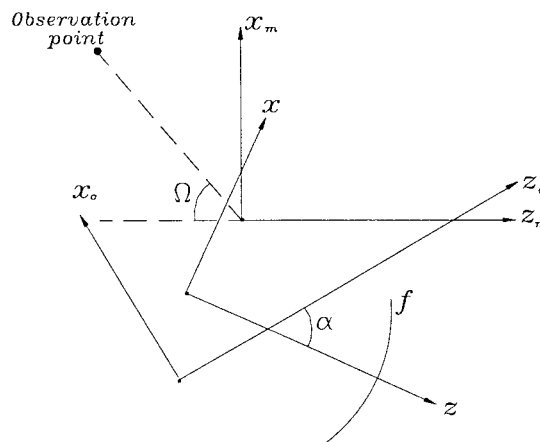


Fig. 1. The relationship among three coordinate systems for analyzing an arbitrary subreflector.

In this paper, the geometrical parameters of an arbitrary-shaped subreflector for UTD analysis are derived using differential geometry. Then, the UTD scattered field patterns of subreflectors are obtained using these parameters. We assume that the reflector surface can be represented by a general coordinate system in order to retain generality. To obtain the GO field, we use the formulation in [10]. To show the validity of our solution, the scattered field pattern of a hyperboloidal reflector is compared with that of UAT. The field patterns of a Gregorian-type-shaped subreflector are also presented.

II. GEOMETRICAL PARAMETERS

A. Geometry of the Reflector

To analyze a subreflector, we introduce three coordinate systems: (x_0, y_0, z_0) , (x, y, z) , and (x_m, y_m, z_m) . The relation between three coordinates are depicted in Fig. 1. To make the problem more general, we assume that the subreflector surface is represented by an arbitrary coordinate system (x_0, y_0, z_0) . The coordinate (x, y, z) , which is used to define the edge of a subreflector, is defined such that the z axis of this coordinate passes through the center of the subreflector and the feed of the antenna is located at the origin of the coordinate system. The coordinate (x_0, y_0, z_0) is tilted by α to (x, y, z) . The coordinate (x_m, y_m, z_m) is the coordinate for a main reflector and the observation points are defined by this coordinate system.

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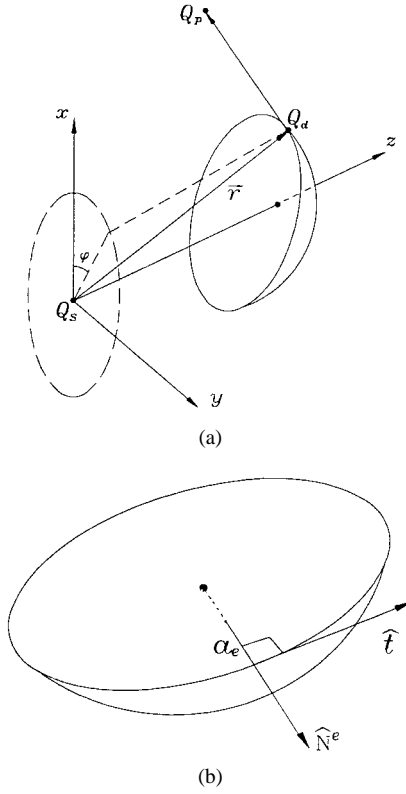


Fig. 2. The geometry of a subreflector. (a) Parametric expression of the edge. (b) Normal and tangential unit vectors on the edge and the radius of curvature of the edge.

The reflector surface is defined in the coordinates \$(x_0, y_0, z_0)\$ as

$$z_0 = f(x_0, y_0). \quad (1)$$

Outward surface unit normal vector \$\hat{N}^0\$ is given in \$(x, y, z)\$ coordinates by

$$\hat{N}^0 = N_1^0 \hat{x} + N_2^0 \hat{y} + N_3^0 \hat{z} \quad (2)$$

where

$$N_1^0 = \frac{f_{x_0} \cos \alpha + \sin \alpha}{\sqrt{f_{x_0}^2 + f_{y_0}^2 + 1}}, \quad N_2^0 = \frac{f_{y_0}}{\sqrt{f_{x_0}^2 + f_{y_0}^2 + 1}}$$

$$N_3^0 = \frac{f_{z_0} \sin \alpha - \cos \alpha}{\sqrt{f_{x_0}^2 + f_{y_0}^2 + 1}}$$

and \$f_x = \partial f / \partial x\$.

B. Differential Geometry of the Edge

To represent the closed contour of the edge illustrated in Fig. 2(a) using the parametric form, we define an edge in the \$(x, y, z)\$ coordinate system as follows:

$$\vec{r} = g_1(\phi) \hat{x} + g_2(\phi) \hat{y} + g_3(\phi) \hat{z} \quad (3)$$

where \$(g_1(\phi), g_2(\phi), g_3(\phi))\$ is the position on the edge for a given value of parameter \$\phi\$ and can be obtained by adopting the same procedure in [10].

The diffraction, source and observation points in \$(x, y, z)\$ coordinates are given as

$$\text{diffraction point } Q_d; (x_d, y_d, z_d) = (g_1(\phi), g_2(\phi), g_3(\phi))$$

$$\text{source point } Q_s; (x_s, y_s, z_s) = (0, 0, 0)$$

$$\text{observation point } Q_p; (x_p, y_p, z_p).$$

The edge parameters are shown in Fig. 2(b) and can be determined from [11]. The unit tangential vector at the edge is

$$\hat{t} = \frac{\vec{r}'}{|\vec{r}'|} = t_1 \hat{x} + t_2 \hat{y} + t_3 \hat{z} \quad (4)$$

where

$$t_i = \frac{g'_i}{\sqrt{g_1'^2 + g_2'^2 + g_3'^2}}, \quad \text{for } i = 1, 2, 3$$

and the prime(') represents the derivative with respect to \$\phi\$.

The unit normal vector and radius of curvature on the edge are given by

$$\hat{N}^e = -\frac{\hat{t}'}{|\hat{t}'|} = N_a^e \hat{x} + N_2^e \hat{y} + N_3^e \hat{z} \quad (5)$$

$$a_e = \frac{|\hat{t}|}{|\hat{t}'|} = \frac{g_1'^2 + g_2'^2 + g_3'^2}{\sqrt{A_1^2 + A_2^2 + A_3^2}} \quad (6)$$

where

$$N_i^e = -\frac{A_i}{\sqrt{A_1^2 + A_2^2 + A_3^2}}, \quad \text{for } i = 1, 2, 3$$

$$A_i = g_i'' - \frac{g_1' g_1'' + g_2' g_2'' + g_3' g_3''}{\sqrt{t_1^2 + t_2^2 + t_3^2}} g_i'.$$

The vector components of the edge-fixed coordinate system for the geometry under consideration are summarized in Table I. Note that the unit vectors \$(\hat{s}^{i,d}, \hat{\phi}^{i,d}, \hat{\beta}^{i,d})\$ correspond to the unit vectors \$(\hat{s}', \hat{\phi}', \hat{\beta}') and \$(\hat{s}, \hat{\phi}, \hat{\beta})\$ in [3], respectively.

C. Other Geometrical Parameters

The angle between the incident ray and the edge is defined by

$$\beta_0^i = \cos^{-1}[\hat{s}^i \cdot \hat{t}] = \cos^{-1}(t_1 s_1^i + t_2 s_2^i + t_3 s_3^i). \quad (7)$$

By Keller's law of diffraction, the angle between the diffracted ray and the edge is the same as \$\beta_0^i\$.

The vector tangential to the surface and normal to the edge is given by

$$\hat{t}^0 = \hat{N}^0 \times \hat{t} = t_1^0 \hat{x} + t_2^0 \hat{y} + t_3^0 \hat{z} \quad (8)$$

where

$$t_1^0 = N_2^0 t_1 - N_3^0 t_2, \quad t_2^0 = N_3^0 t_1 - N_1^0 t_3$$

$$t_3^0 = N_1^0 t_2 - N_2^0 t_1.$$

TABLE I
THE COMPONENTS OF THE EDGE-FIXED COORDINATE SYSTEMS. (a) THE INCIDENT RAY. (b) THE DIFFRACTED RAY

$\hat{s}^i =$	s_1^i	s_2^i	s_3^i	s^i
$s_1^i \hat{x} + s_2^i \hat{y} + s_3^i \hat{z}$	$\frac{x_d - x_s}{s^i}$	$\frac{y_d - y_s}{s^i}$	$\frac{z_d - z_s}{s^i}$	$\{(x_d - x_s)^2 + (y_d - y_s)^2 + (z_d - z_s)^2\}^{1/2}$
$\hat{\phi}^i =$	ϕ_1^i	ϕ_2^i	ϕ_3^i	ϕ^i
$\phi_1^i \hat{x} + \phi_2^i \hat{y} + \phi_3^i \hat{z}$	$\frac{s_2^i t_3 - s_3^i t_2}{\phi^i}$	$\frac{s_3^i t_1 - s_1^i t_3}{\phi^i}$	$\frac{s_1^i t_2 - s_2^i t_1}{\phi^i}$	$\{(s_2^i t_3 - s_3^i t_2)^2 + (s_3^i t_1 - s_1^i t_3)^2 + (s_1^i t_2 - s_2^i t_1)^2\}^{1/2}$
$\hat{\beta}^i =$	β_1^i	β_2^i	β_3^i	β^i
$\beta_1^i \hat{x} + \beta_2^i \hat{y} + \beta_3^i \hat{z}$	$\phi_2^i s_3^i - \phi_3^i s_2^i$	$\phi_3^i s_1^i - \phi_1^i s_3^i$	$\phi_1^i s_2^i - \phi_2^i s_1^i$	1

(a)

$\hat{s}^d =$	s_1^d	s_2^d	s_3^d	s^d
$s_1^d \hat{x} + s_2^d \hat{y} + s_3^d \hat{z}$	$\frac{x_p - x_d}{s^d}$	$\frac{y_p - y_d}{s^d}$	$\frac{z_p - z_d}{s^d}$	$\{(x_p - x_d)^2 + (y_p - y_d)^2 + (z_p - z_d)^2\}^{1/2}$
$\hat{\phi}^d =$	ϕ_1^d	ϕ_2^d	ϕ_3^d	ϕ^d
$\phi_1^d \hat{x} + \phi_2^d \hat{y} + \phi_3^d \hat{z}$	$\frac{s_2^d t_3 - s_3^d t_2}{\phi^d}$	$\frac{s_3^d t_1 - s_1^d t_3}{\phi^d}$	$\frac{s_1^d t_2 - s_2^d t_1}{\phi^d}$	$\{(s_2^d t_3 - s_3^d t_2)^2 + (s_3^d t_1 - s_1^d t_3)^2 + (s_1^d t_2 - s_2^d t_1)^2\}^{1/2}$
$\hat{\beta}^d =$	β_1^d	β_2^d	β_3^d	β^d
$\beta_1^d \hat{x} + \beta_2^d \hat{y} + \beta_3^d \hat{z}$	$\phi_2^d s_3^d - \phi_3^d s_2^d$	$\phi_3^d s_1^d - \phi_1^d s_3^d$	$\phi_1^d s_2^d - \phi_2^d s_1^d$	1

(b)

The unit vector \hat{s}_t^i , which lies in the incident plane and perpendicular to \hat{t} , is obtained as

$$\hat{s}_t^i = \hat{s}_1^{it} \hat{x} + \hat{s}_2^{it} \hat{y} + \hat{s}_3^{it} \hat{z} \quad (9)$$

where

$$s_j^{it} = \frac{\cos \beta_0 t_j - s_j^i}{\sin \beta_0}, \quad \text{for } j = 1, 2, 3.$$

Simiarly, \hat{s}_t^d , which lies in the diffraction plane and is perpendicular to \hat{t}' , is given by

$$\hat{s}_t^d = \hat{s}_1^{dt} \hat{x} + \hat{s}_2^{dt} \hat{y} + \hat{s}_3^{dt} \hat{z} \quad (10)$$

where

$$s_j^{dt} = \frac{s_j^d - \cos \beta_0}{\sin \beta_0}, \quad \text{for } j = 1, 2, 3.$$

The angle ϕ_0^i , the angle between $-\hat{s}_t^i$ and \hat{t}_0 , is given by

$$\phi_0^i = \pi - [\pi - \cos^{-1}(-\hat{s}_t^i \cdot \hat{t}_0)] \text{sgn}(-\hat{s}_t^i \cdot \hat{N}^0). \quad (11)$$

Also, ϕ_0^d , the angle between $-\hat{s}_t^d$ and \hat{t}_0 , is expressed as

$$\phi_0^d = \pi - [\pi - \cos^{-1}(-\hat{s}_t^d \cdot \hat{t}_0)] \text{sgn}(\hat{s}_t^d \cdot \hat{N}^0). \quad (12)$$

The radii of curvature a_1 (tangential to the incident plane) and a_2 (perpendicular to the incident plane) are obtained

as

$$a_{1,2} = \frac{EB_1^2 \pm 2FB_1B_2 + GB_2^2}{eB_1^2 \pm 2fB_1B_2 + gB_2^2}, \quad (\text{+for } a_1 \text{ and } - \text{for } a_2) \quad (13)$$

where

$$B_1 = s_1^i \cos \alpha + s_1^i \sin \alpha + (-s_1^i \sin \alpha + s_2^i \cos \alpha) f_{x_0}$$

$$B_2 = s_2^i + (-s_1^i \sin \alpha + s_3^i \cos \alpha) f_{y_0}$$

$$E = 1 + f_{x_0}^2, \quad F = f_{x_0} f_{y_0}, \quad G = 1 + f_{y_0}^2$$

$$e = \frac{-f_{x_0 x_0}}{\Delta}, \quad f = \frac{-f_{x_0 y_0}}{\Delta}, \quad g = \frac{-f_{y_0 y_0}}{\Delta}$$

$$\Delta = \sqrt{f_{x_0}^2 + f_{y_0}^2 + 1}.$$

III. SCATTERED FIELD FORMULATION

Most of the reflector antennas (except for multifocal antennas) have single-reflection points and multiple-diffraction points. The total scattered field at the obserbation point Q_p is the simple vector addition of individual field components. Therefore, the scattered field \vec{E}^{scat} can be expressed as

$$\vec{E}^{\text{scat}}(Q_p) = \vec{E}^r(Q_p) + \sum_{n=1}^{N_d} \vec{E}_n^d(Q_p) \quad (15)$$

where \vec{E}^r is the reflected field obtained by GO and \vec{E}_n^d is the n th diffracted field in the UTD expression. N_d is number of the diffraction points.

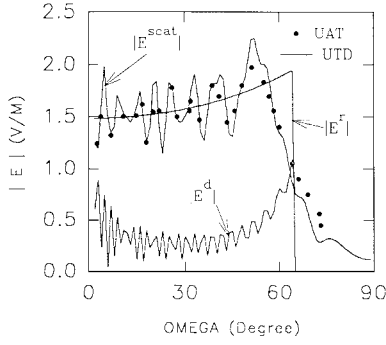


Fig. 3. Comparison of radiation patterns of the symmetric hyperboloidal reflector obtained by UAT and UTD.

In order to obtain the GO field, it is necessary to determine the reflection point for a given observation point. For classical dual reflector antennas, the reflection point can be found easily from the fact that every reflected ray must pass through one focal point. However, for shaped dual reflector antennas, the subreflector does not have a focal point. Therefore, the reflection point on the subreflector of these antennas should be found by utilizing the stationary property of the path length at the reflection point. The GO field can be determined by the GO expressions given in [10].

To obtain the UTD diffracted fields, we should define the edge profile (g_1, g_2, g_3) numerically. The diffraction points can be found by applying Keller's law of diffraction to the edge. For a given diffraction point, the UTD parameters (for example, distance parameter, caustic distance, etc.) can be determined by the geometrical parameters obtained in Section II; then we can evaluate the diffracted field using the UTD parameters. Since the UTD formulations are presented in [12], we do not repeat them here.

IV. NUMERICAL ANALYSIS

A. Symmetric Hyperboloidal Subreflector

A hyperboloidal reflector is widely used as a subreflector for a Cassegrain antenna. To show the validity of our analysis, we compare the scattered field pattern of the symmetric hyperboloidal reflector is given by [10, Eq. 5.2].

We assume that the field incident upon the surface of a subreflector is given by

$$\vec{E}^i(r, \theta, \phi) = \frac{120\pi}{(r/\lambda)} e^{-jkr} [\sin \phi \hat{\theta} + \cos \phi \hat{\phi}]. \quad (16)$$

The observation points are far away from the center of the coordinate (x_m, y_m, z_m) system at a distance of 100λ .

The scattered field patterns of the subreflector obtained by UTD and by UAT are compared in Fig. 3. There is no significant difference between two results. Also, we can observe that UTD diffracted fields eliminate the discontinuity of the GO field.

B. Offset-Shaped Subreflector

The surface profile of a shaped dual offset-reflector antenna is defined numerically and the sampling points are nonuni-

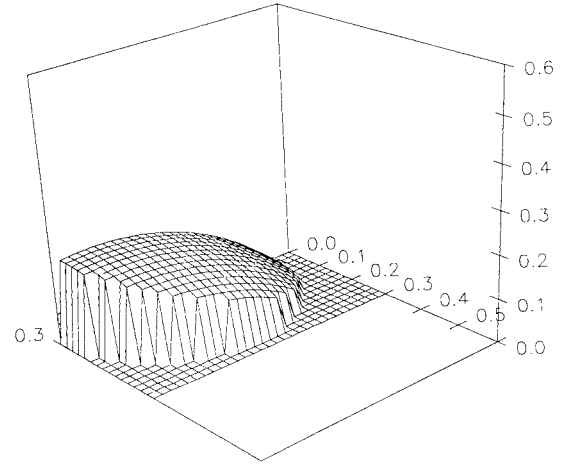


Fig. 4. Profile of the shaped subreflector represented by the global interpolation.

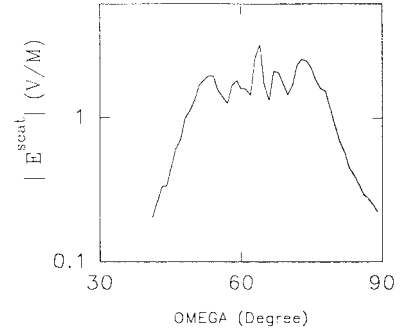


Fig. 5. Radiation pattern of the shaped subreflector obtained by UTD.

formly distributed. Conventionally, a surface is represented in closed form (quadratic formulation, for example) with a perturbation function [13]. Recently, the global interpolation method has been developed [14]. In this method, the analytic surface function can be obtained by expanding the surface in terms of the orthogonal functions. The surface characteristic is determined from the set of coefficients of the series.

The subreflector considered here is that of the shaped offset Gregorian-type antenna system, which has a circular aperture, the left-right symmetry, and no tilted structure [15], [16]. The design data of the reflector is presented in [16] and the reflector profile is depicted in Fig. 4. Since the system has left-right symmetry, only half of the reflector is presented. In this case, the surface defined coordinate (x_0, y_0, z_0) system is coincident with the coordinate (x_m, y_m, z_m) system. We transformed the discrete reflector profiles into the analytic function by expanding in terms of the Jacobi polynomial sinusoidal functions [14].

It is difficult to determine the first and the second derivatives on the shaped subreflector accurately and smoothly. We overcome these difficulties by applying the local interpolation technique [14]. Furthermore, the modified Powell's method is utilized in finding the reflection point on the subreflector and the cost function used in this algorithm is defined by the reciprocal of path length [17]. The radiation field pattern of this reflector is shown in Fig. 5.

V. CONCLUSION

The subreflector of a dual offset-reflector antenna system has been analyzed by UTD. Geometrical parameters of an arbitrary shaped subreflector were derived by using differential geometry. By applying these parameters to the UTD field formulation, the diffracted field from the subreflector was evaluated. The GO fields were obtained by using the same formulas as the UAT. In the numerical computation, two types of subreflectors have been considered. The scattered field pattern of the symmetric hyperboloidal reflector shows a good agreement with UAT result. The field pattern of the shaped subreflector represented by global interpolation was presented. In the above two cases, one can observe that the UTD diffracted fields eliminate the discontinuities of GO fields at the shadow boundaries.

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