# Solubility and Diffusivity of Nitrous Oxide in Ternary Mixtures of Water, Monoethanolamine, and N-Methyldiethanolamine and Solution Densities and Viscosities

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The densities and viscosities of aqueous N-methyldiethanolamine/monoethanolamine (MDEA/MEA) blends containing 30 and 40 mass % total amine with MEA concentrations of 5, 10, and 15 mass % of the total amine concentration were measured at temperatures of 303, 313, and 323 K. The diffusion coefficients and Henry's law constants of  $N_2O$  in these solutions were also measured and were used to estimate the diffusion coefficients and Henry's law constants of  $CO_2$  in these solutions according to the " $N_2O/CO_2$  analogy" technique.

#### Introduction

Recently, several researchers have suggested using aqueous mixtures of small amounts of monoethanolamine (MEA) and much larger amounts of N-methyldiethanolamine (MDEA) for the absorption of CO<sub>2</sub> and for the selective removal of  $H_2S$  from gas streams of mixtures of  $CO_2$  and  $H_2S$  (1-5). The objective of this paper is to provide values for some of the physical properties which are needed for the analysis of experimentally acquired data for the absorption of CO<sub>2</sub> into aqueous solutions of mixtures of MEA and MDEA. These physical properties are also needed for predicting the absorption rates and enhancement factors of CO2 into aqueous blends of MDEA and MEA which are useful to process engineers who are interested in the problem of acid gas removal by aqueous blends of MEA and MDEA. The physical properties that were measured are the densities and viscosities of aqueous MDEA/MEA blends containing 30 and 40 mass % total amine with MEA concentrations of 5, 10, and 15 mass % of the total amine concentration at temperatures of 303, 313, and 323 K. The diffusion coefficients and Henry's law constants of N<sub>2</sub>O in these solutions were also measured and were used to estimate the diffusion coefficients and Henry's law constants of CO<sub>2</sub> in these solutions according to the " $N_2O/CO_2$  analogy" technique (6). The experimental apparatus and procedures that were used in our laboratory for these measurements have been described in detail previously (6). The MDEA was purchased from Union Carbide with a purity of 99% or better, and the MEA was purchased from Fisher with a purity of 95% or better.

### **Results and Correlations**

The equilibrium concentration of  $CO_2$  in the liquid,  $u_{CO_2}$ , is related to its partial pressure in the gas phase,  $P_{CO_2}$ , by Henry's law constant,  $H_{CO_2}$ , according to the following equation:

$$u_{\mathrm{CO}_2} = P_{\mathrm{CO}_2} / H_{\mathrm{CO}_2} \tag{1}$$

Since CO<sub>2</sub> reacts in aqueous amine solutions, the solubility and diffusivity of CO<sub>2</sub> cannot be measured directly. In

Table 1. Henry's Law Constants and Diffusion Coefficients of  $N_2O$  and  $CO_2$  in Pure Water

T/K	$\begin{array}{c} H^{\mathrm{o}}\mathrm{N_{2O}}^{}\prime}/\\ \mathrm{(MPa\cdot m^{3\bullet}kmol^{-1})} \end{array}$	$H^{0}_{\text{CO}_{2}}^{a/}$ $(\text{MPa·m}^{3}\text{·kmol}-1)$	$^{10^9D^o_{N_2O}{}^a/}_{(m^2-s^{-1})}$	$^{10^9D^o{}_{CO_2}{}^b/}_{(m^2s^{-1})}$
303	4.35	3.39	1.607	2.16
313	5.02	4.25	1.679	2.71
323	5.37	5.17	1.868	3.34

<sup>&</sup>lt;sup>a</sup> Reference 6. <sup>b</sup> Reference 8.

this work, the solubility and diffusivity of  $N_2O$  in aqueous MDEA/MEA mixtures were measured. The  $N_2O/CO_2$  analogy technique (7) can then be employed to estimate the solubility and diffusivity of  $CO_2$  in these mixtures. The similarity between  $CO_2$  and  $N_2O$  in mass, molecular structure, and molecular interaction parameters led Clarke (7) to assume that the ratios of the solubilities or diffusivities of  $CO_2$  and  $N_2O$  in water and in aqueous solutions of organic solvents are similar within 5% or better at the same temperature. Hence, according to the  $N_2O/CO_2$  analogy, Henry's law constants of  $CO_2$  and  $N_2O$  in the aqueous amine solutions and in pure water and the diffusion coefficients of  $CO_2$  and  $N_2O$  in the aqueous amine solutions and in pure water are related by the following equations:

$$H_{\rm CO_2}/H_{\rm CO_2}^{\rm o} = H_{\rm N_2O}/H_{\rm N_2O}^{\rm o}$$
 (2)

$$D_{\rm CO_2}/D_{\rm CO_2}^{\circ} = D_{\rm N_2O}/D_{\rm N_2O}^{\circ}$$
 (3)

where superscript o refers to pure water. The values of Henry's law constants and diffusion coefficients of  $N_2O$  and  $CO_2$  in pure water are reported in Table 1.

The densities and viscosities of aqueous MDEA/MEA blends containing 30 and 40 mass % total amine with MEA concentrations of 5, 10, and 15 mass % of the total amine concentration were measured at temperatures of 303, 313, and 323 K and are reported in Tables 2 and 3, respectively. Henry's law constants and the diffusion coefficients of  $N_2O$  in these solutions were measured and are reported in Tables 4 and 5, respectively. Henry's law constants and diffusion coefficients of  $CO_2$  which were estimated from eqs 2 and 3 are reported in Tables 6 and 7, respectively. These properties were correlated as functions of temperature and

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Table 2. Density  $\varrho$  of Aqueous MDEA/MEA Solutions

	$10^{-3}\varrho/(\text{kgm}-3)$ at $w_{\text{MDEA}}/w_{\text{MEA}} =$										
T/K	$0.30/0^{a}$	0.285/0.015	0.27/0.03	0.255/0.045	$0.40/0^a$	0.38/0.02	0.36/0.04	0.34/0.06			
303	1.0229	1.021 72	1.021 19	1.020 28	1.0322	1.030 90	1.030 18	1.029 36			
313	1.0180	$1.016\ 56$	1.01507	1.013 94	1.0266	$1.025\ 21$	$1.024\ 41$	1.02375			
323	1.0130	1.010 43	1.009 69	1.009 12	1.0204	$1.019\ 27$	$1.018\ 24$	1.017 76			

<sup>&</sup>lt;sup>a</sup> Reference 6.

Table 3. Viscosity  $\mu$  of Aqueous MDEA/MEA Solutions

	$10^3 \mu / (\text{kgm}^{-1} \cdot \text{s}^{-1})$ at $w_{\text{MDEA}} / w_{\text{MEA}} =$										
T/K	$0.30/0^{a}$	0.285/0.015	0.27/0.03	0.255/0.045	$0.40/0^a$	0.38/0.02	0.36/0.04	0.34/0.06			
303	2.612	2.601	2.559	2.542	4.359	4.279	4.189	4.097			
313	1.937	1.944	1.915	1.892	3.112	3.035	3.011	2.913			
323	1.505	1.506	1.490	1.477	2.309	2.255	2.241	2.214			

<sup>&</sup>lt;sup>a</sup> Reference 6.

Table 4. Henry's Law Constants for N<sub>2</sub>O in Aqueous MDEA/MEA Solutions

	$H_{\rm N_2O}/({ m MPa\cdot m^3\cdot kmol}-1)$ at $w_{ m MDEA}/w_{ m MEA}=$										
T/K	$0.30/0^{a}$	0.285/0.015	0.27/0.03	0.255/0.045	$0.40/0^a$	0.38/0.02	0.36/0.04	0.34/0.06			
303	5.10	5.14	5.27	5.36	5.43	5.58	5.67	5.85			
313	5.90	6.10	6.29	6.48	6.21	6.27	6.34	6.44			
323	6.07	6.35	6.55	6.59	6.22	6.29	6.32	6.43			

<sup>&</sup>lt;sup>a</sup> Reference 6.

Table 5. Diffusion Coefficients of N2O in Aqueous Solutions of MDEA/MEA

	$10^9 D_{\rm N_2O}/({\rm m^2 \cdot s^{-1}})$ at $w_{\rm MDEA}/w_{\rm MEA} =$									
T/K	$0.30/0^{a}$	0.285/0.015	0.27/0.03	0.255/0.045	$0.40/0^a$	0.38/0.02	0.36/0.04	0.34/0.06		
303	1.032	1.136	1.267	1.393	0.824	0.844	0.905	0.973		
313	1.240	1.265	1.345	1.450	1.108	1.159	1.207	1.288		
323	1.421	1.488	1.564	1.656	1.269	1.305	1.391	1.471		

<sup>&</sup>lt;sup>a</sup> Reference 6.

Table 6. Estimated Henry's Law Constants for  $CO_2$  in Aqueous MDEA/MEA Solutions According to the  $N_2O/CO_2$  Analogy Technique

	$H_{\rm CO}/({ m MPa\cdot m^3\cdot kmol^{-1}})$ at $w_{\rm MDEA}/w_{\rm MEA}=$									
T/K	$0.30/0^{a}$	0.285/0.015	0.27/0.03	0.255/0.045	$0.40/0^a$	0.38/0.02	0.36/0.04	0.34/0.06		
303	3.98	4.01	4.11	4.18	4.24	4.35	4.43	4.56		
313	4.99	5.17	5.32	5.49	5.25	5.31	5.36	5.46		
323	5.84	6.11	6.30	6.34	5.99	6.05	6.08	6.18		

<sup>&</sup>lt;sup>a</sup> Reference 6.

 $\begin{tabular}{ll} Table 7. Estimated Diffusion Coefficients of CO_2 in Aqueous Solutions of MDEA/MEA According to the $N_2O/CO_2$ Analogy Technique \\ \end{tabular}$ 

	$10^9 D_{\rm CO}/(\rm m^2 s^{-1})$ at $w_{\rm MDEA}/w_{\rm MEA} =$									
T/K	$0.30/0^{a}$	0.285/0.015	0.27/0.03	0.255/0.045	$0.40/0^{a}$	0.38/0.02	0.36/0.04	0.34/0.06		
303	1.387	1.545	1.723	1.895	1.108	1.148	1.231	1.323		
313	2.001	2.047	2.176	2.346	1.788	1.875	1.953	2.084		
323	2.541	2.665	2.801	2.966	2.264	2.337	2.491	2.634		

<sup>&</sup>lt;sup>a</sup> Reference 6.

concentration according to the following equations:

solubility (Henry's law constant) of N2O

$$\label{eq:ln} \ln(H_{\rm N_2O}/({\rm MPa\cdot m^3\cdot kmol}^{-1})) = A_1 + B_1/(T/{\rm K}) \qquad (4)$$
 estimated solubility (Henry's law constant) of  ${\rm CO_2}$ 

$$ln(H_{CO_2}/(MPa \cdot m^3 \cdot kmol^{-1})) = A_2 + B_2/(T/K)$$
 (5)

density  $\varrho$  of aqueous MDEA/MEA solution

$$\varrho/(kgm^{-3}) = A_3 + B_3(T/K)$$
 (6)

viscosity  $\mu$  of aqueous MDEA/MEA solution

$$\ln(\mu/(\text{kg·m}^{-1}\cdot\text{s}^{-1})) = A_4 + B_4/(T/K)$$
 (7)

 $A_k$  and  $B_k$  are correlated with the mass fractions of MDEA ( $w_{\text{MDEA}}$ ) and MEA ( $w_{\text{MEA}}$ ) in the solution according to the following equations:

$$A_k = a_k + b_k w_{\text{MDEA}} + c_k w_{\text{MEA}} \tag{8}$$

$$B_k = d_k + e_k w_{\text{MDEA}} + f_k w_{\text{MEA}} \tag{9}$$

The values of the constants  $a_k$ ,  $b_k$ ,  $c_k$ ,  $d_k$ ,  $e_k$ , and  $f_k$  are

Table 8. Constant Coefficients for Calculating  $A_k$  and  $B_k$ , k = 1-4, Which Are Required in Eqs 4-7

	$A_k =$	$= a_k + b_k w_{\text{MDEA}} + c_k v_k$	$B_k$	$B_k = d_k + e_k w_{\text{MDEA}} + f_k w_{\text{MEA}}$			
$\boldsymbol{k}$	$a_{\mathrm{k}}$	$b_{\mathrm{k}}$	$c_{\mathrm{k}}$	$\overline{d_{\mathrm{k}}}$	$e_{\mathbf{k}}$	fk	
1	9.007562	-13.34430	-15.10479	-2288.484	4236.726	5133.326	
2	12.14463	-13.39581	-15.20839	-3317.018	4252.902	5165.193	
3	1124.340	204.8350	283.2410	-0.4311301	-0.3575680	-0.7899637	
4	-12.19713	-8.905239	-4.823588	1438.717	4218.749	2697.360	

Table 9. Constant Coefficients for Calculating the Diffusion Coefficients of N2O and CO2 in Aqueous Solutions of MDEA/MEA According to Eqs 10 and 11 Along with the Mean Deviations for These Equations

	$D_{ m N_2O}$ /(m²·s-	$\alpha^{-1}$ = $\alpha(\mu/(kgm -$	$(T/K)^{1-s}$	$D_{\text{CO}_2}/(\text{m}^2 \cdot \text{s}^{-1}) = \gamma (\mu/(\text{kg·m}^{-1} \cdot \text{s}^{-1}))^{\delta} (T/K)$			
$w_{ ext{MDEA}}/w_{ ext{MEA}}$	α	β	mean deviation/%	γ	δ	mean deviation/%	
0.30/0	$2.145301 \times 10^{-13}$	-0.4654931	0.55	$1.313257 \times 10^{-14}$	-0.9862939	1.78	
0.285/0.015	$3.999079 \times 10^{-13}$	-0.3742148	1.54	$2.700742 \times 10^{-14}$	-0.8801191	0.33	
0.27/0.03	$8.381405 \times 10^{-13}$	-0.2666473	2.29	$5.431339 \times 10^{-14}$	-0.7780113	1.12	
0.255/0.045	$1.409513 \times 10^{-12}$	-0.1952480	2.30	$9.219197 \times 10^{-14}$	-0.7044025	1.24	
0.40/0	$1.166238 \times 10^{-13}$	-0.5833275	3.03	$1.394693 \times 10^{-14}$	-1.030384	4.45	
0.38/0.02	$1.164062 \times 10^{-13}$	-0.5869788	3.76	$1.518429 \times 10^{-14}$	-1.018302	4.89	
0.36/0.04	$1.213190 \times 10^{-13}$	-0.5886689	2.75	$1.485901 \times 10^{-14}$	-1.029997	4.00	
0.34/0.06	$1.390204 \times 10^{-13}$	-0.5740574	2.40	$1.604657 \times 10^{-14}$	-1.023848	3.33	

reported in Table 8 for k = 1-4. The mean deviations for eqs 4-7 are 2.70%, 1.61%, 0.03%, and 0.64%, respectively. The diffusion coefficients of N2O and CO2 were correlated according to the following equations:

diffusivity of N<sub>2</sub>O

$$D_{\rm N_2O}/({\rm m^2 \cdot s^{-1}}) = \alpha (\mu/({\rm kg \cdot m^{-1} \cdot s^{-1}}))^{\beta} (T/{\rm K}) \eqno(10)$$

estimated diffusivity of CO2

$$D_{\text{CO}}/(\text{m}^2 \cdot \text{s}^{-1}) = \gamma (\mu/(\text{kg} \cdot \text{m}^{-1} \cdot \text{s}^{-1}))^{\delta} (T/\text{K})$$
 (11)

The values of  $\alpha$ ,  $\beta$ ,  $\gamma$ , and  $\delta$  along with the mean deviations for eqs 10 and 11 are reported in Table 9.

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